

Merge Sort

SORTING ALGORITHM

Merge Sort Approach

To sort an array $A[p \dots r]$:

Divide

- Divide the n -element sequence to be sorted into two subsequences of $n/2$ elements each

Conquer

- Sort the subsequences recursively using merge sort
- When the size of the sequences is 1 there is nothing more to do

Combine

- Merge the two sorted subsequences

Merge Sort

Alg.: MERGE-SORT(A, p, r)

if $p < r$

then $q \leftarrow \lfloor (p + r)/2 \rfloor$

MERGE-SORT(A, p, q)

MERGE-SORT($A, q + 1, r$)

MERGE(A, p, q, r)

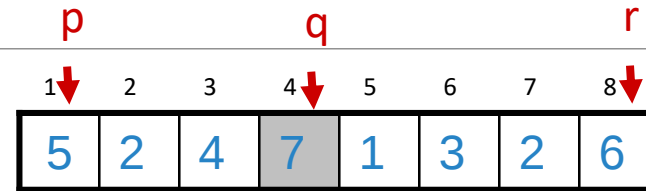
▷ Check for base case

▷ Divide

▷ Conquer

▷ Conquer

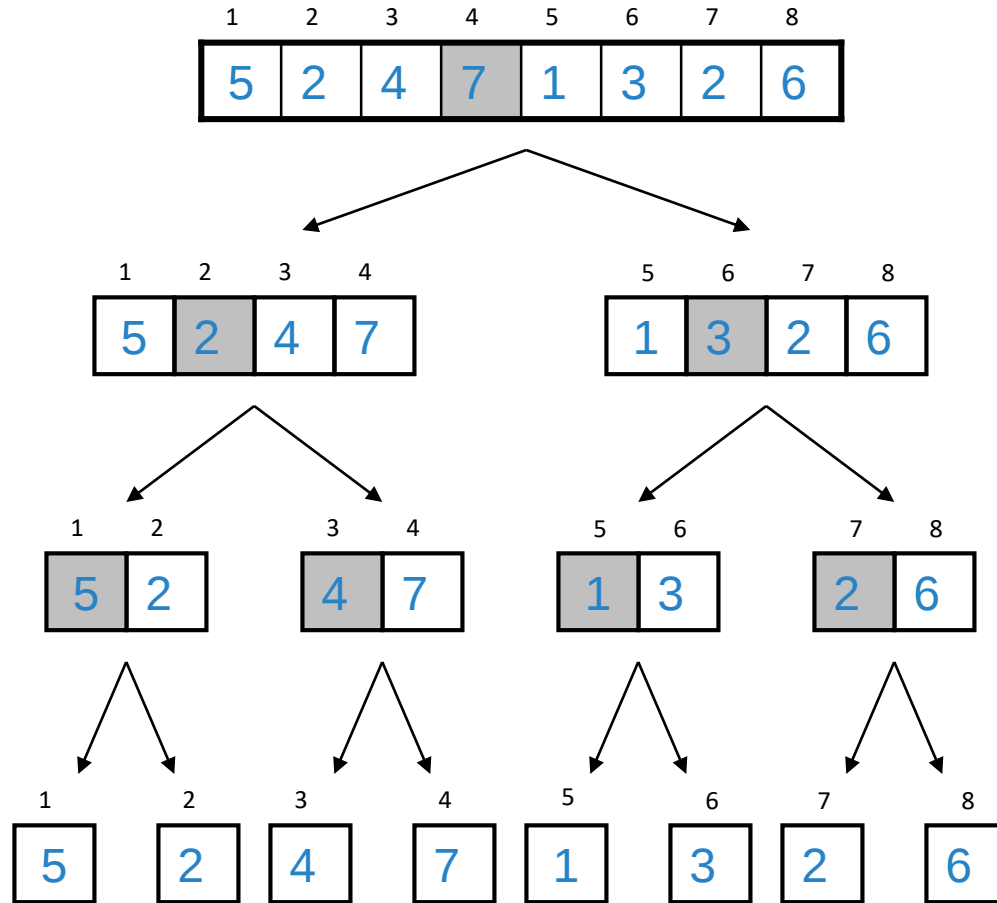
▷ Combine



Initial call: MERGE-SORT($A, 1, n$)

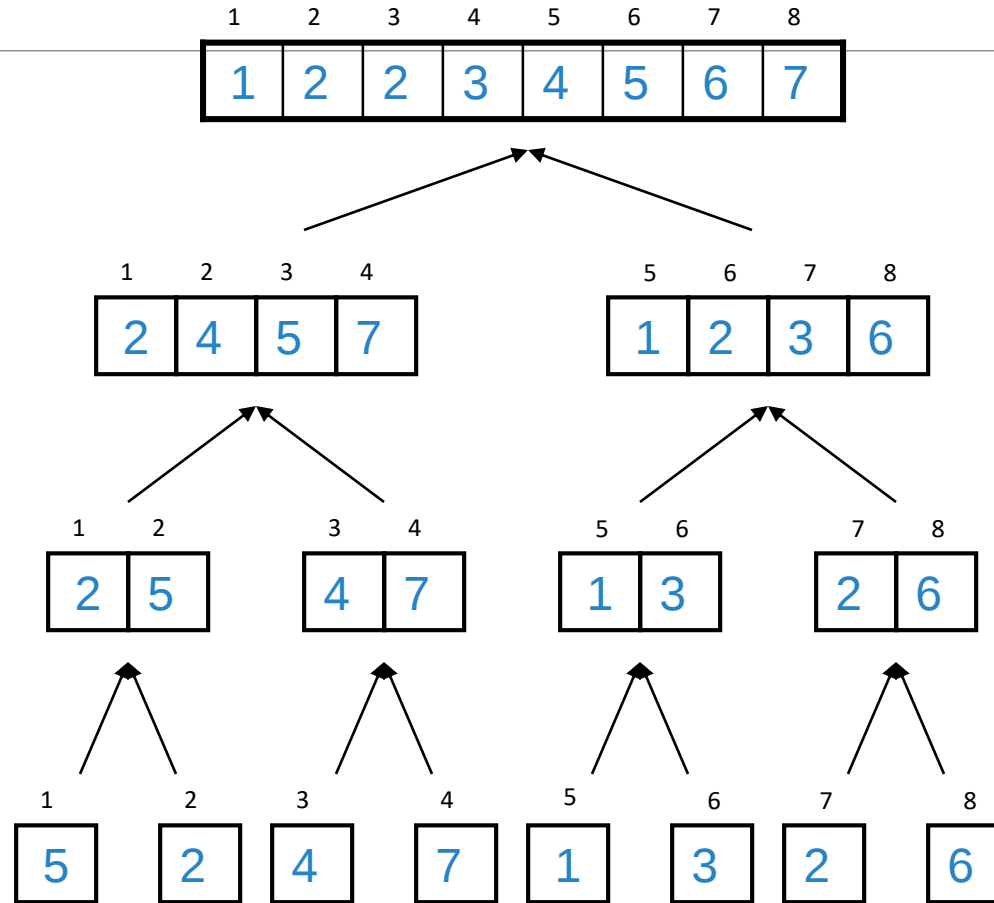
Example – n Power of 2

Divide


$$q = 4$$

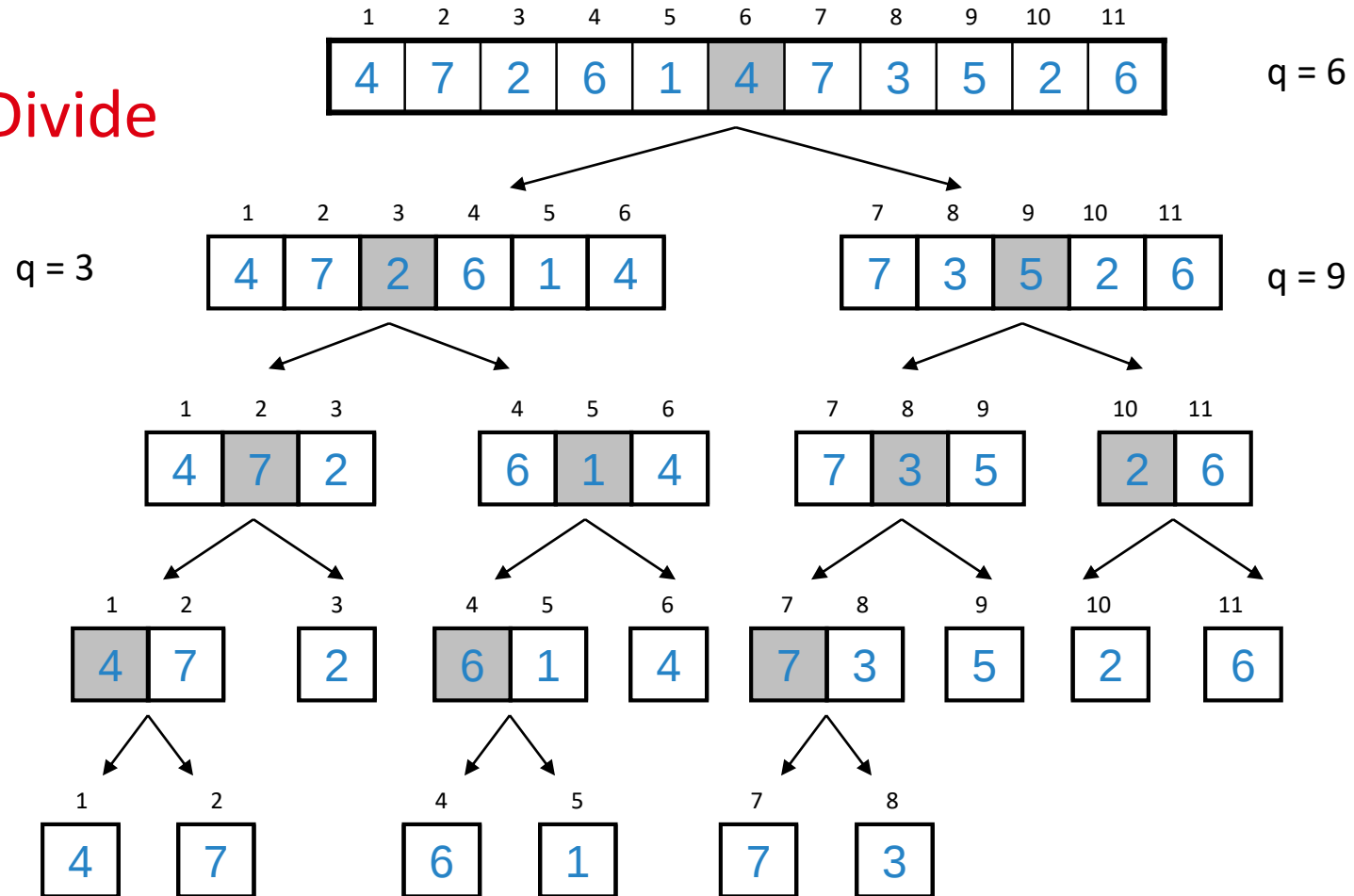
Example – n Power of 2

Conquer
and
Merge



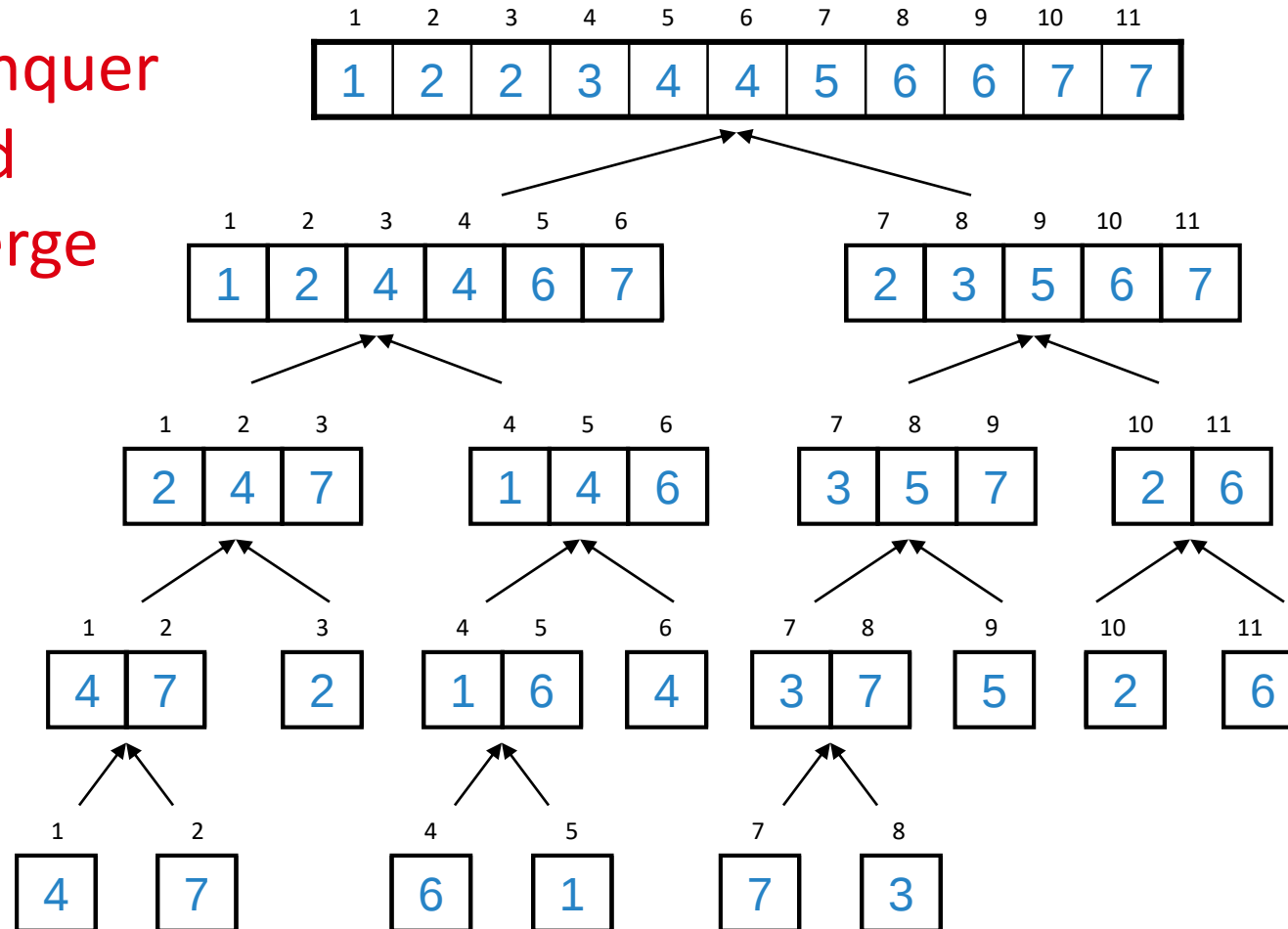
Example – n Not a Power of 2

Divide

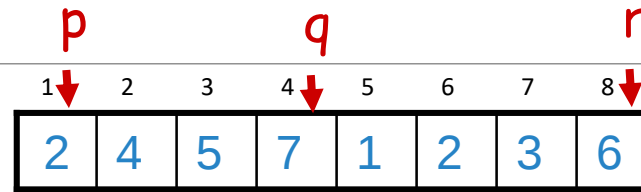


Example – n Not a Power of 2

Conquer
and
Merge



Merging



Input: Array A and indices p, q, r such that $p \leq q < r$

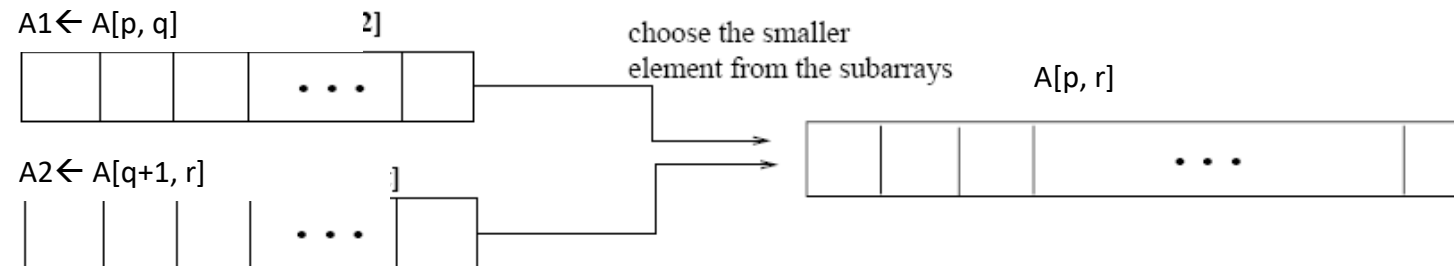
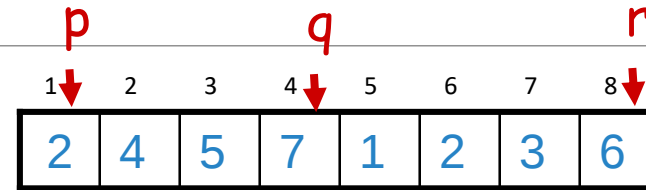
- Subarrays $A[p..q]$ and $A[q+1..r]$ are sorted

Output: One single sorted subarray $A[p..r]$

Merging

Idea for merging:

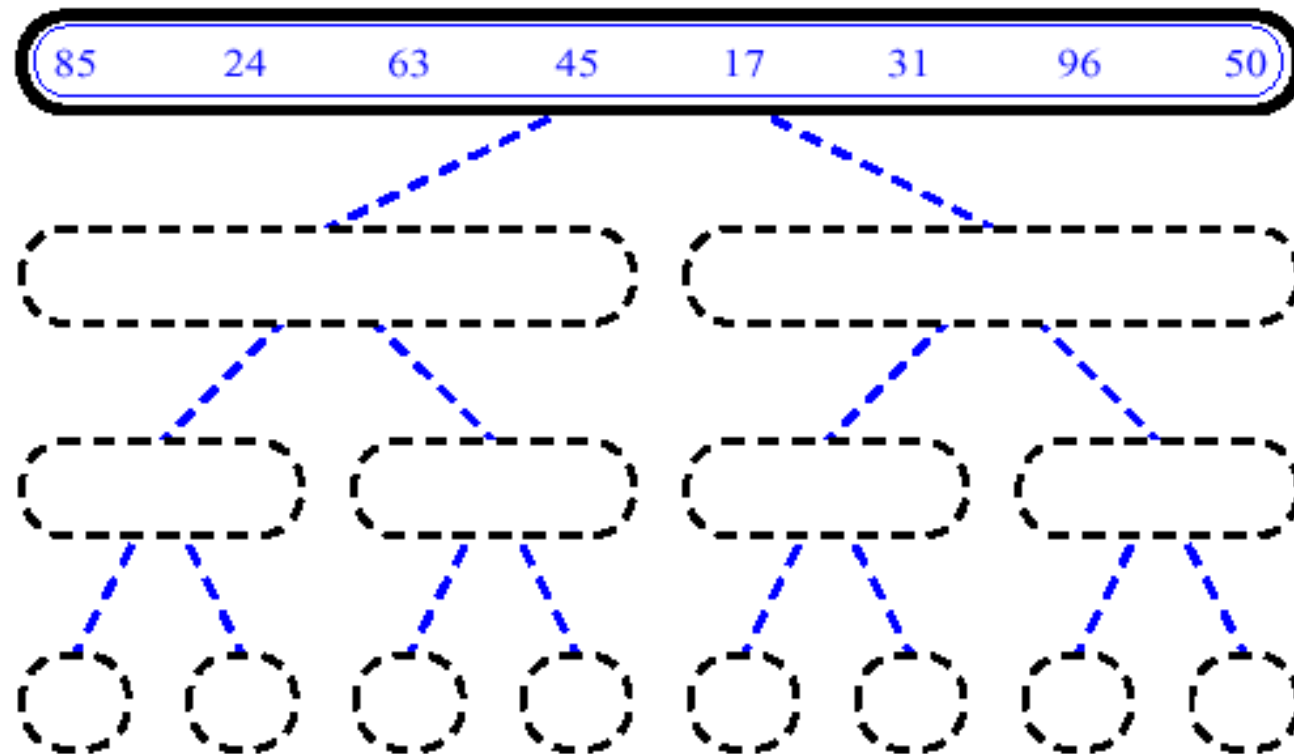
- Two piles of sorted cards
 - Choose the smaller of the two top cards
 - Remove it and place it in the output pile
- Repeat the process until one pile is empty
- Take the remaining input pile and place it face-down onto the output pile



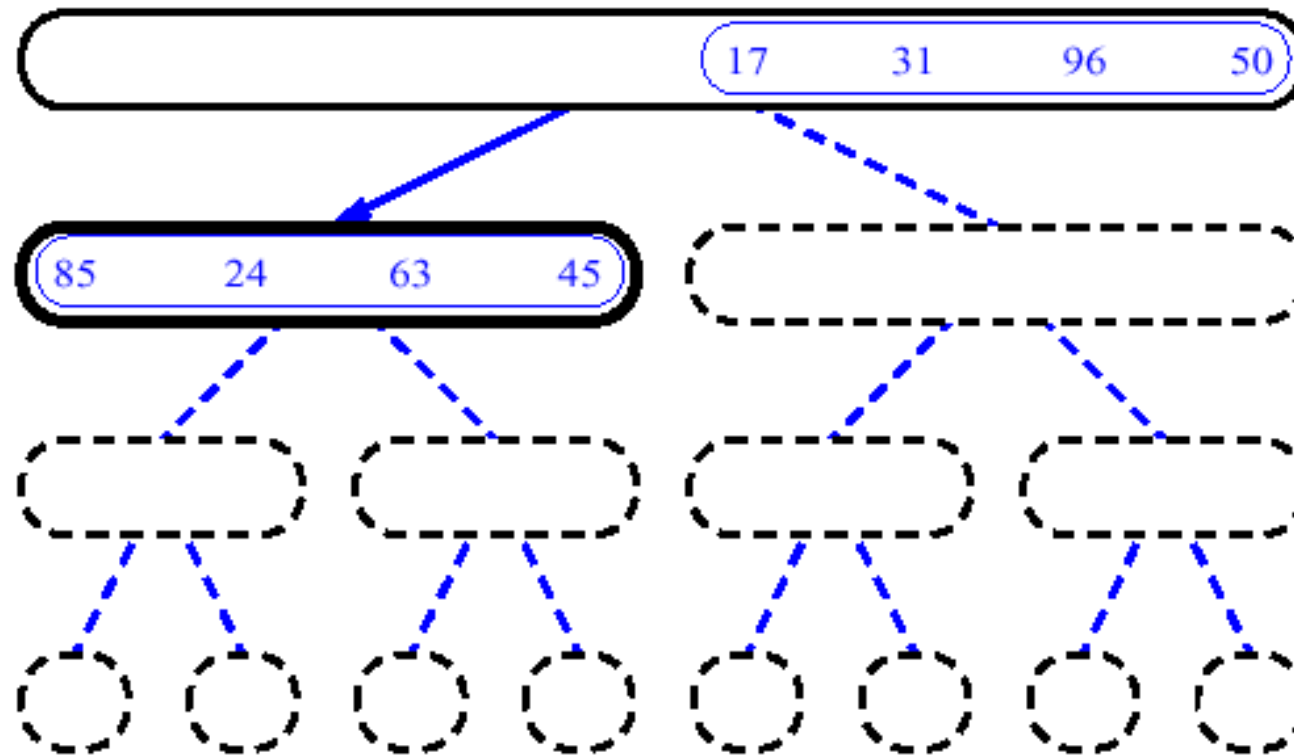
Merge Sort

EXAMPLE

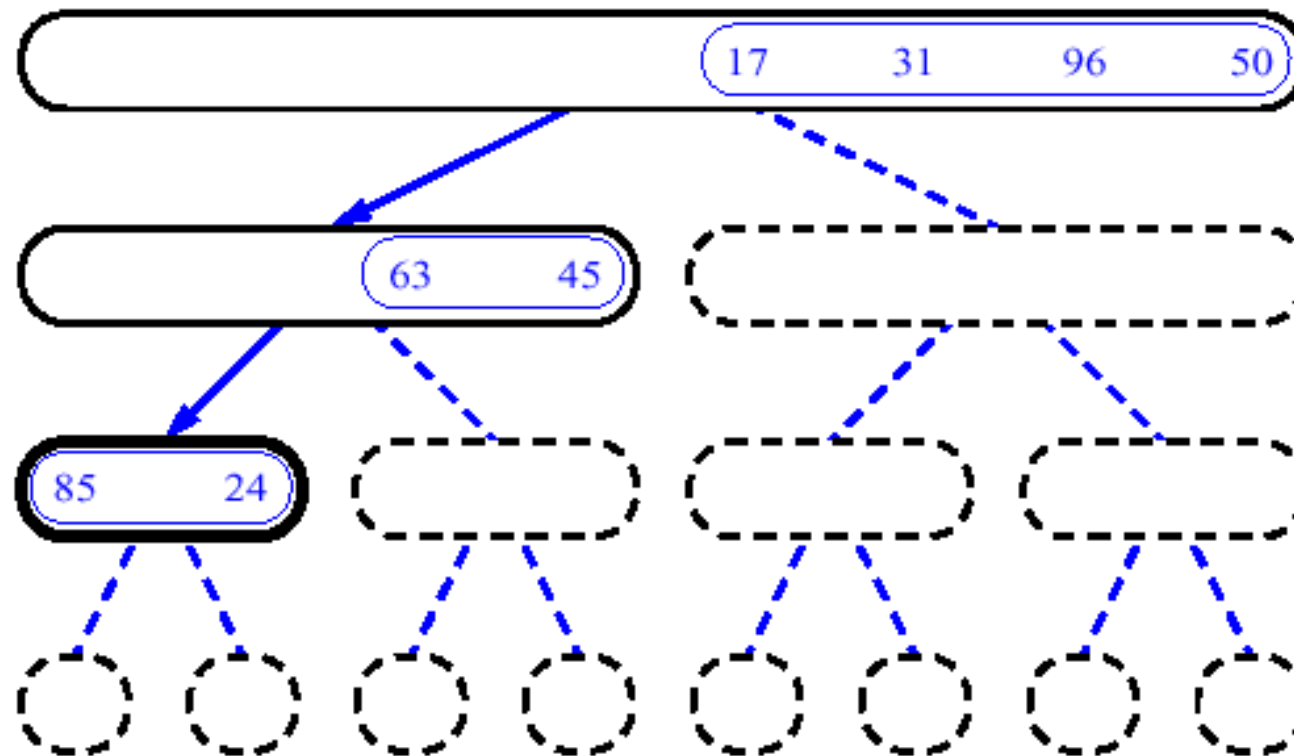
MergeSort (Example) - 1



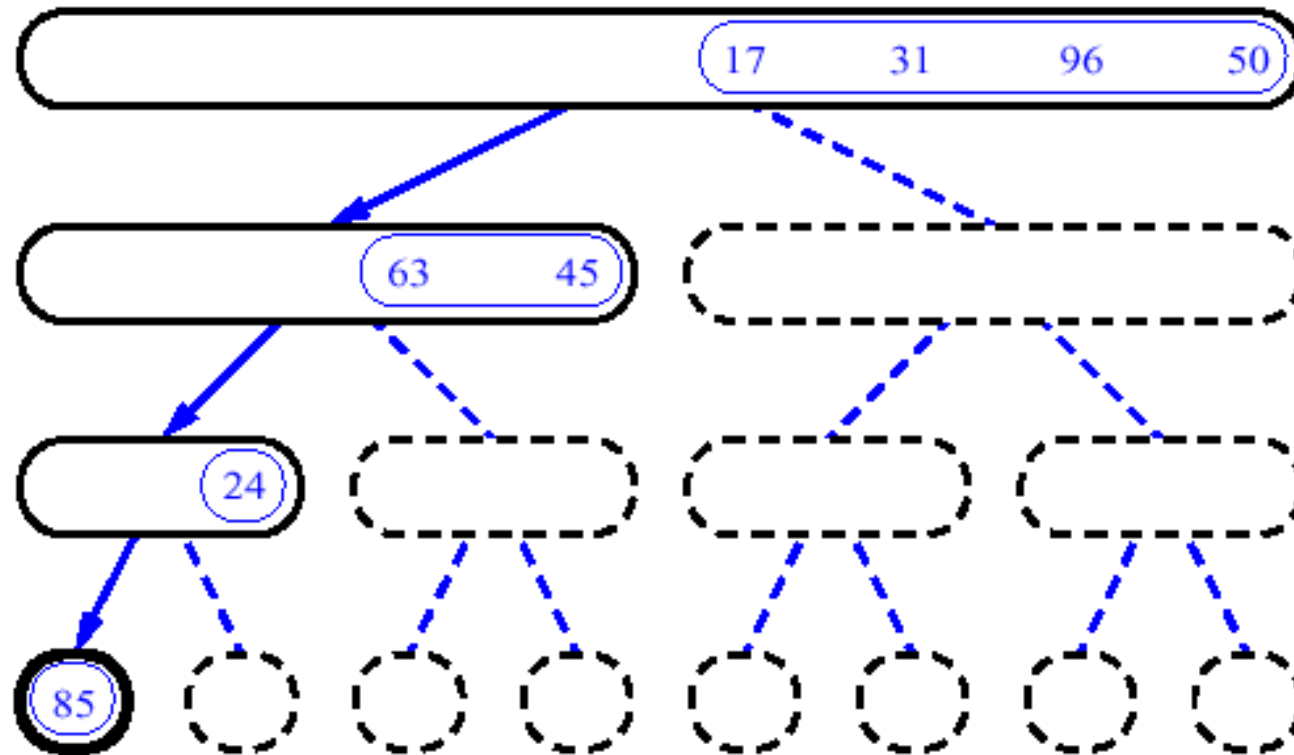
MergeSort (Example) - 2



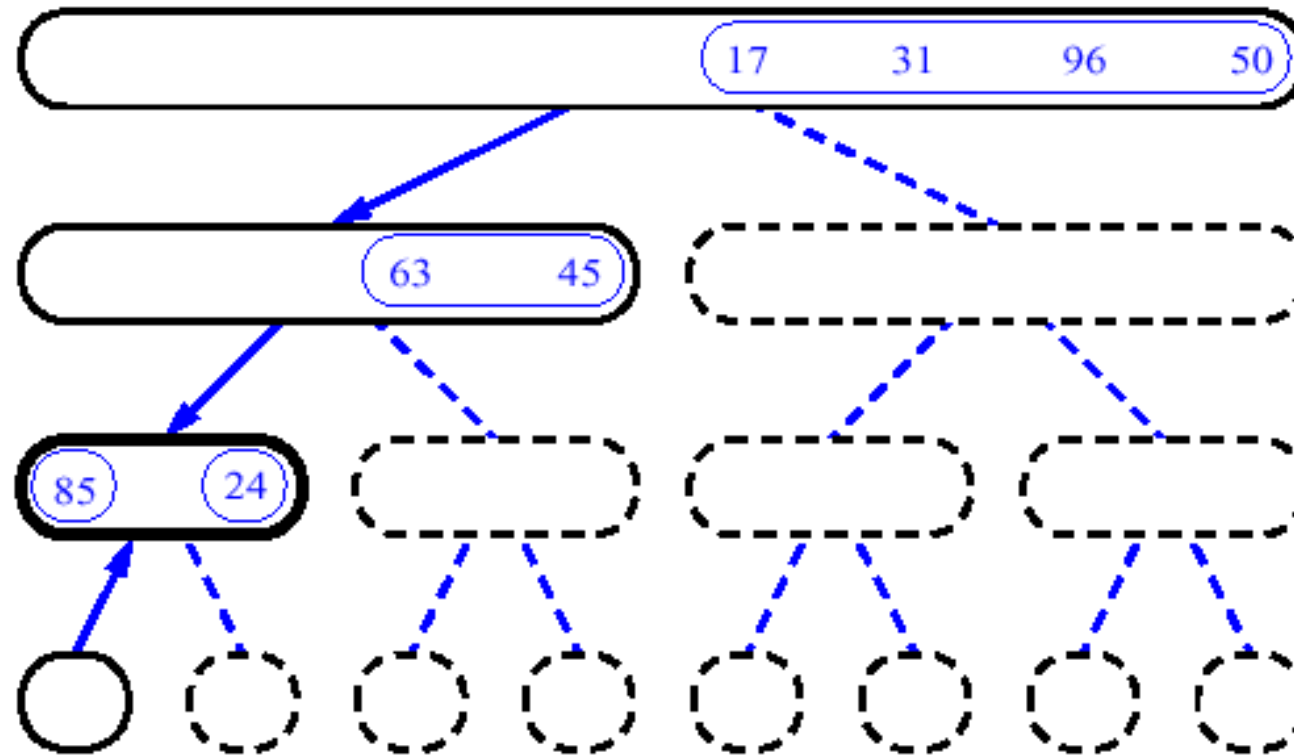
MergeSort (Example) - 3



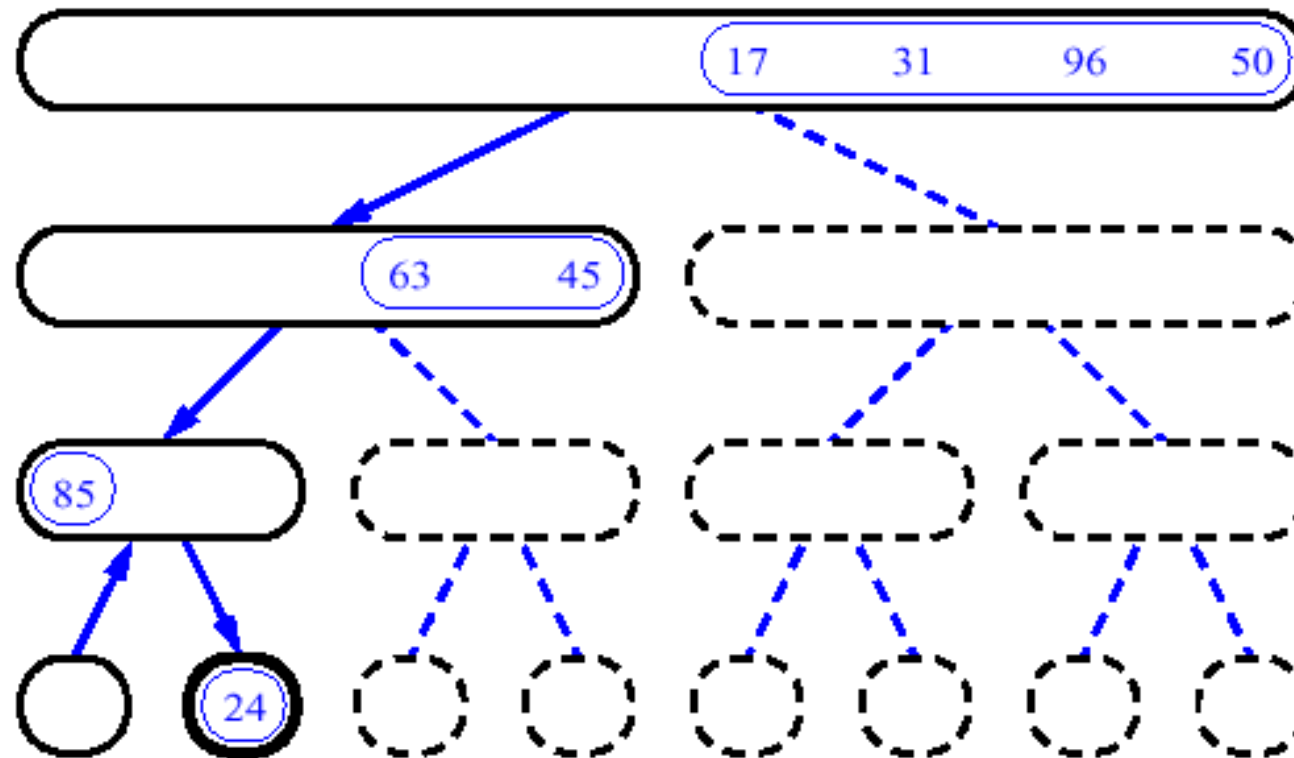
MergeSort (Example) - 4



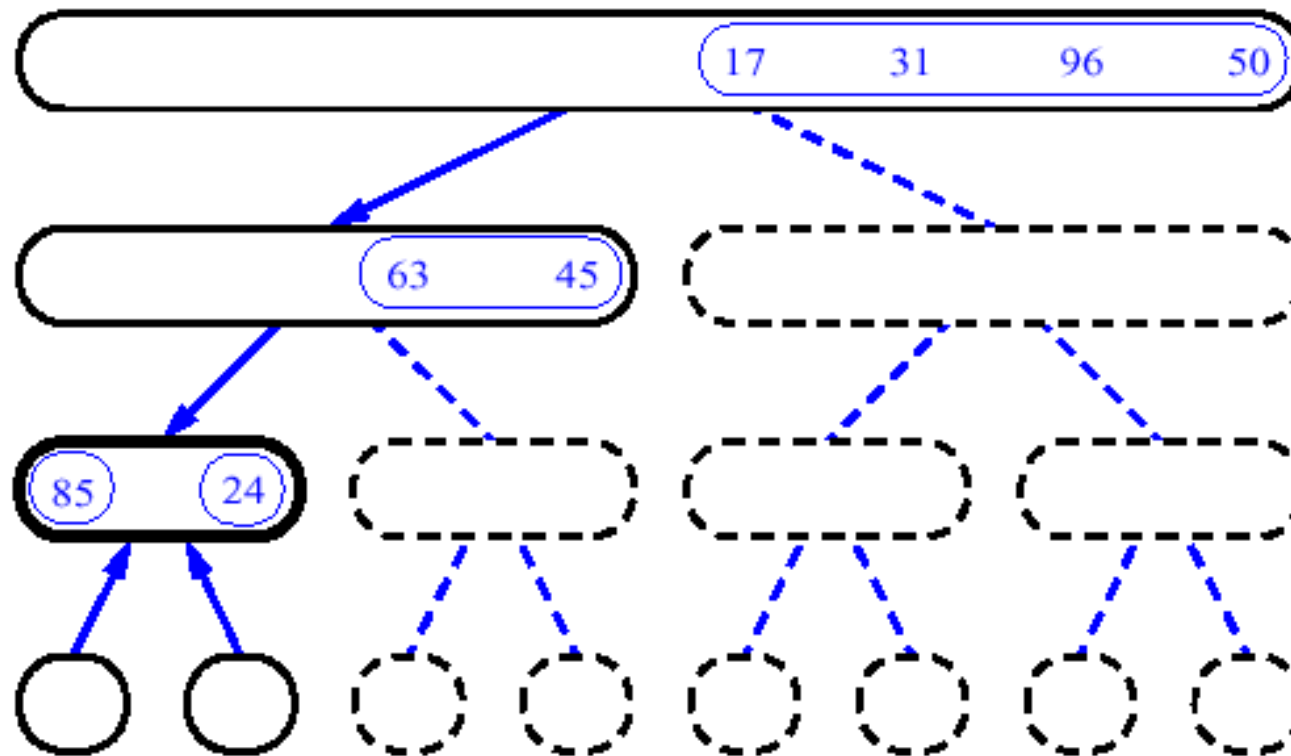
MergeSort (Example) - 5



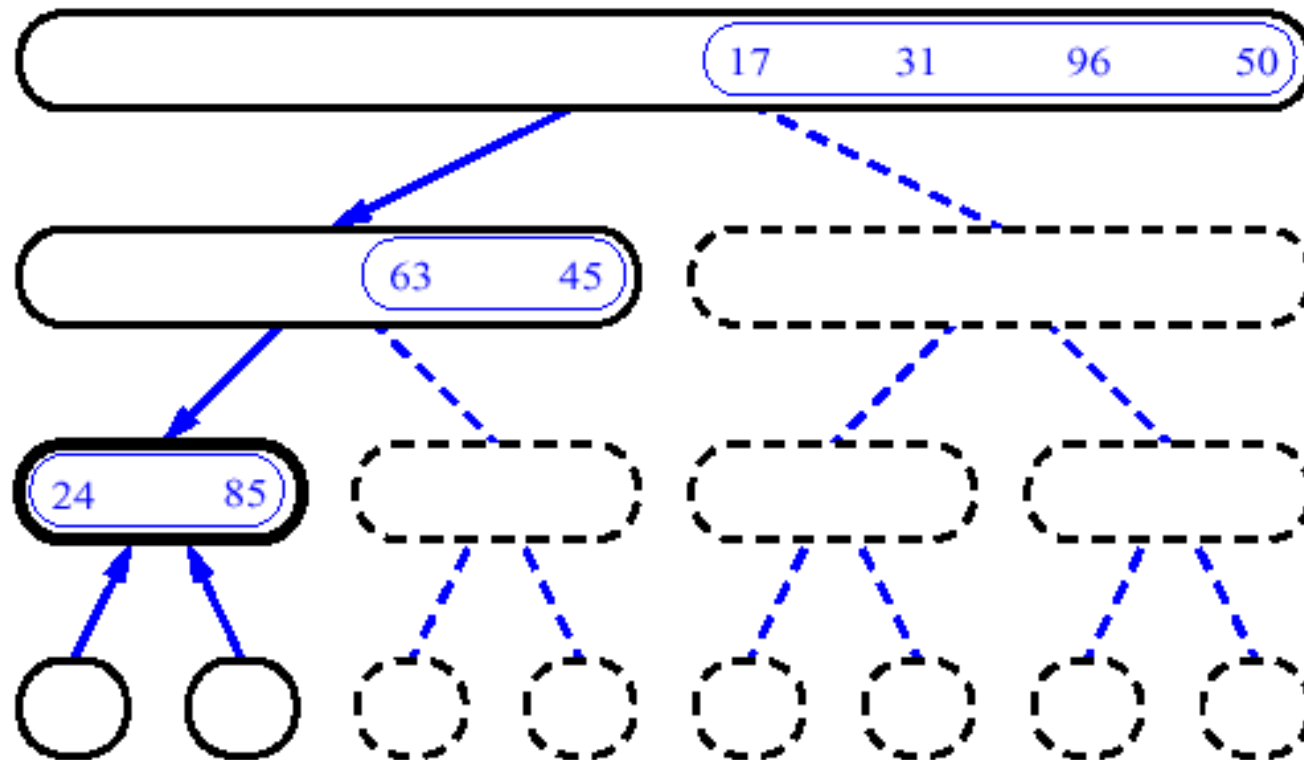
MergeSort (Example) - 6



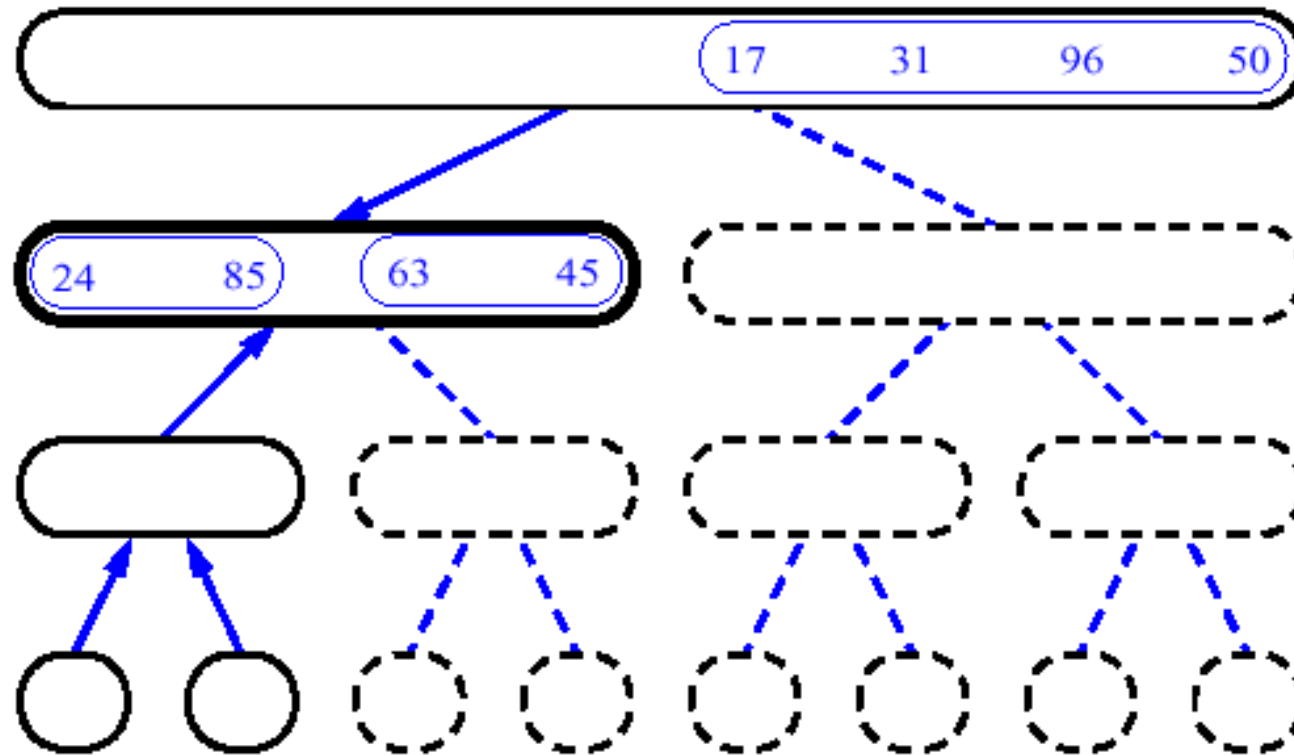
MergeSort (Example) - 7



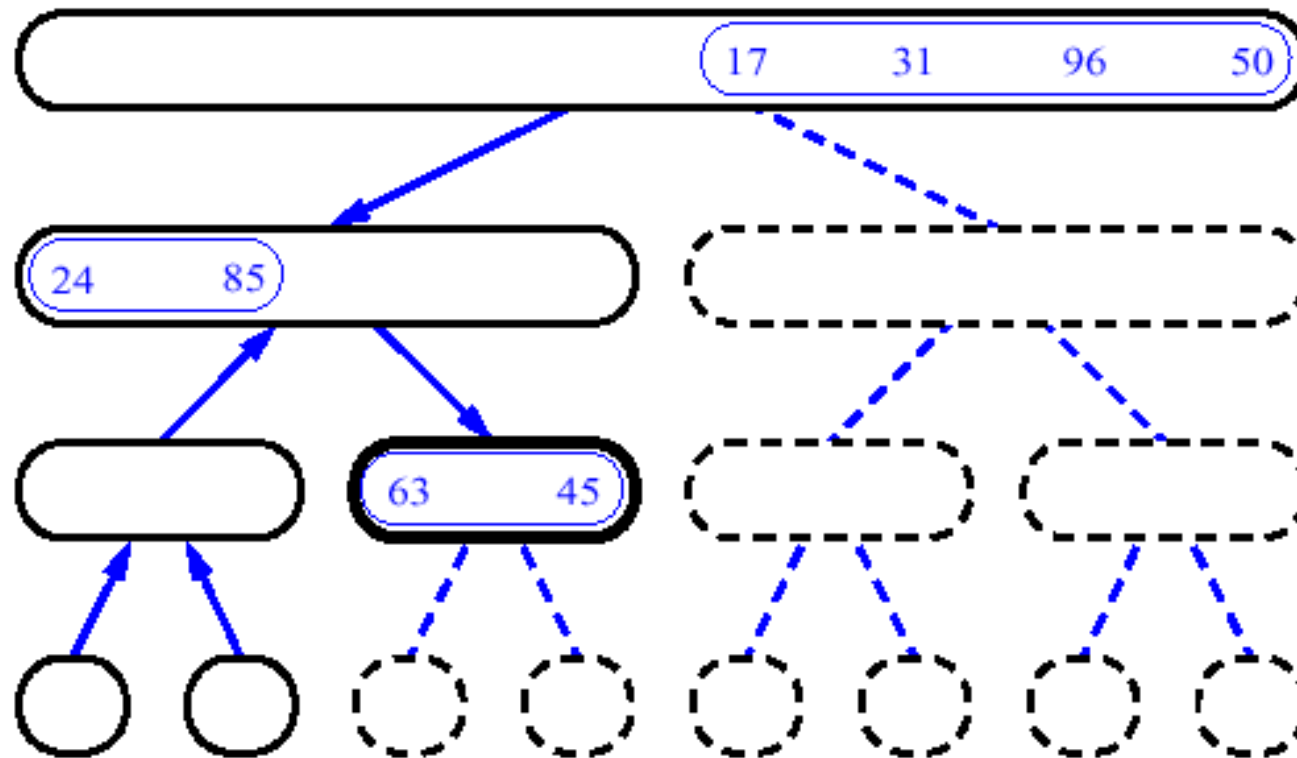
MergeSort (Example) - 8



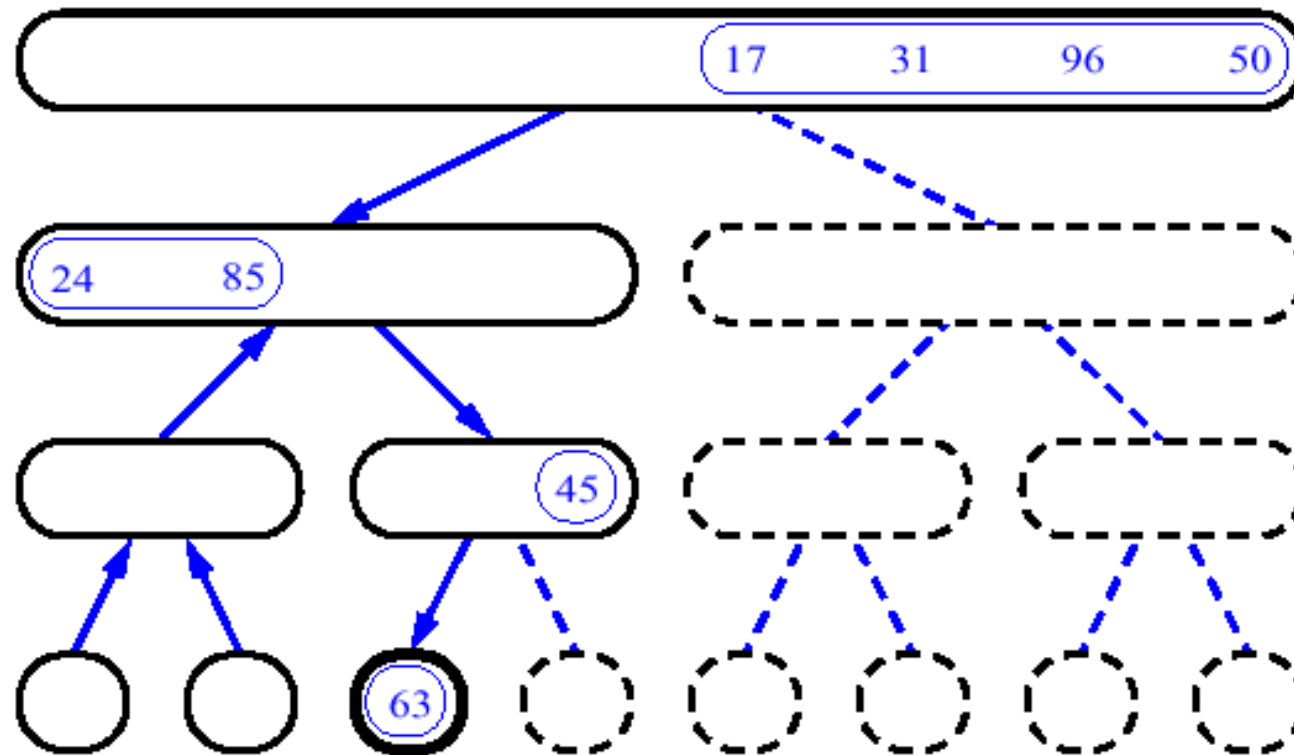
MergeSort (Example) - 9



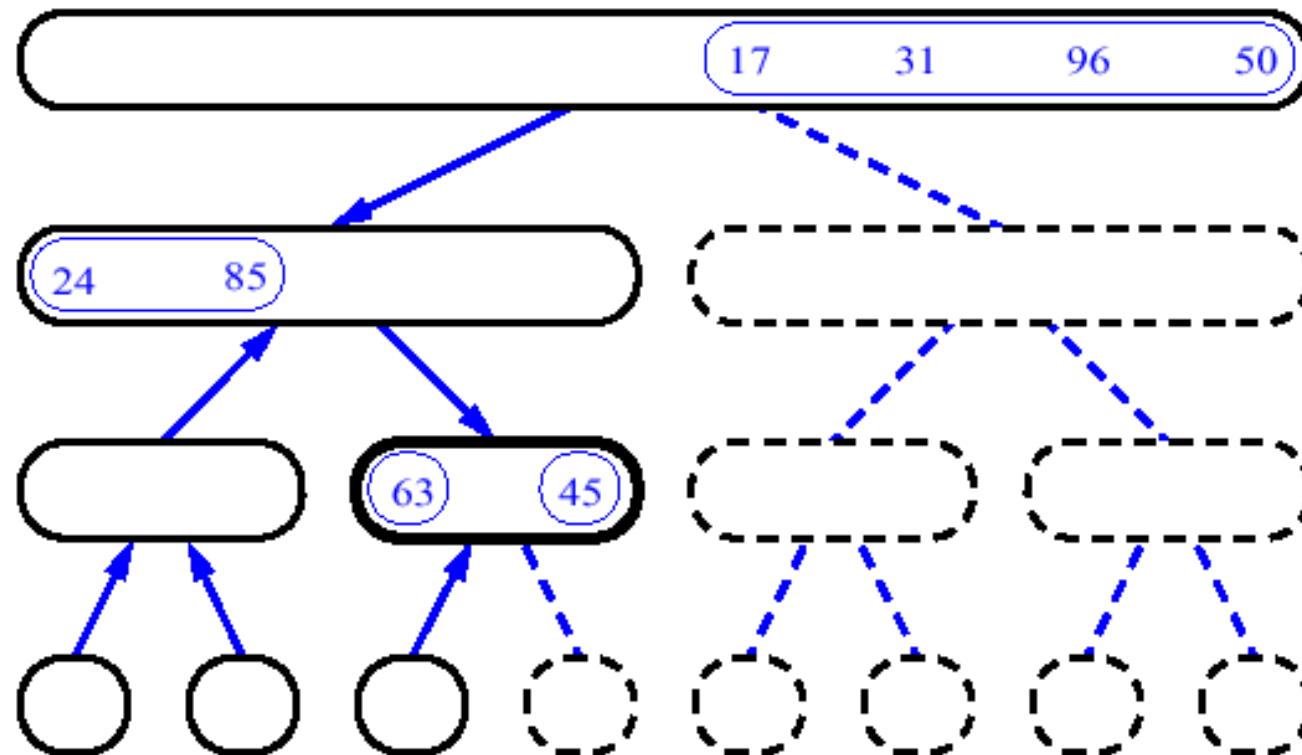
MergeSort (Example) - 10



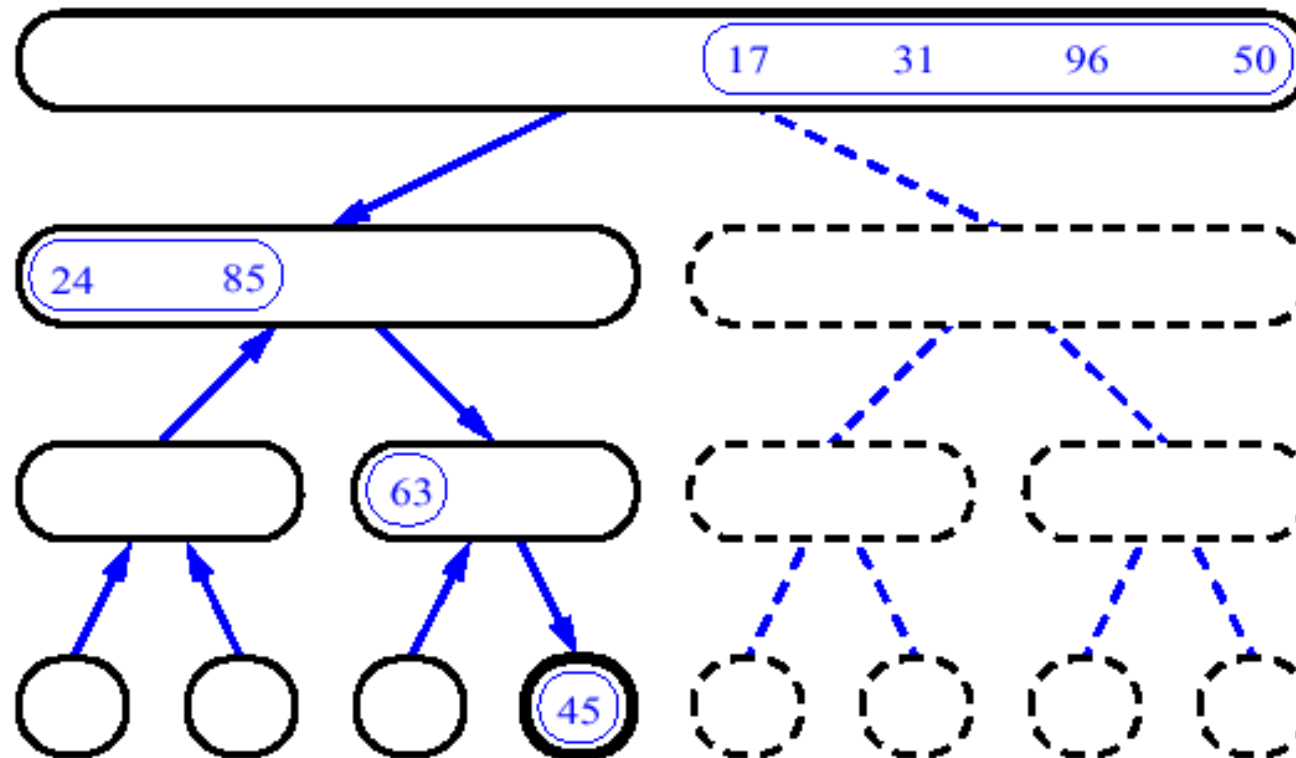
MergeSort (Example) - 11



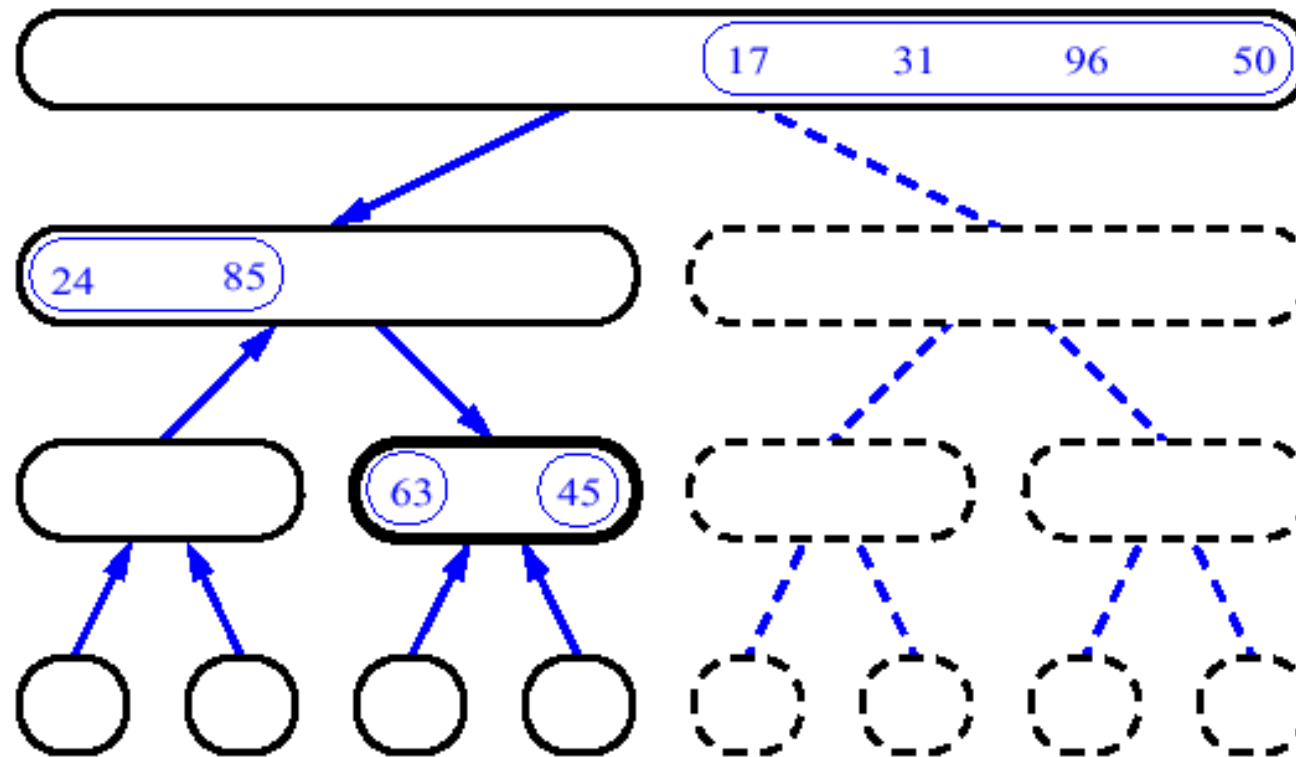
MergeSort (Example) - 12



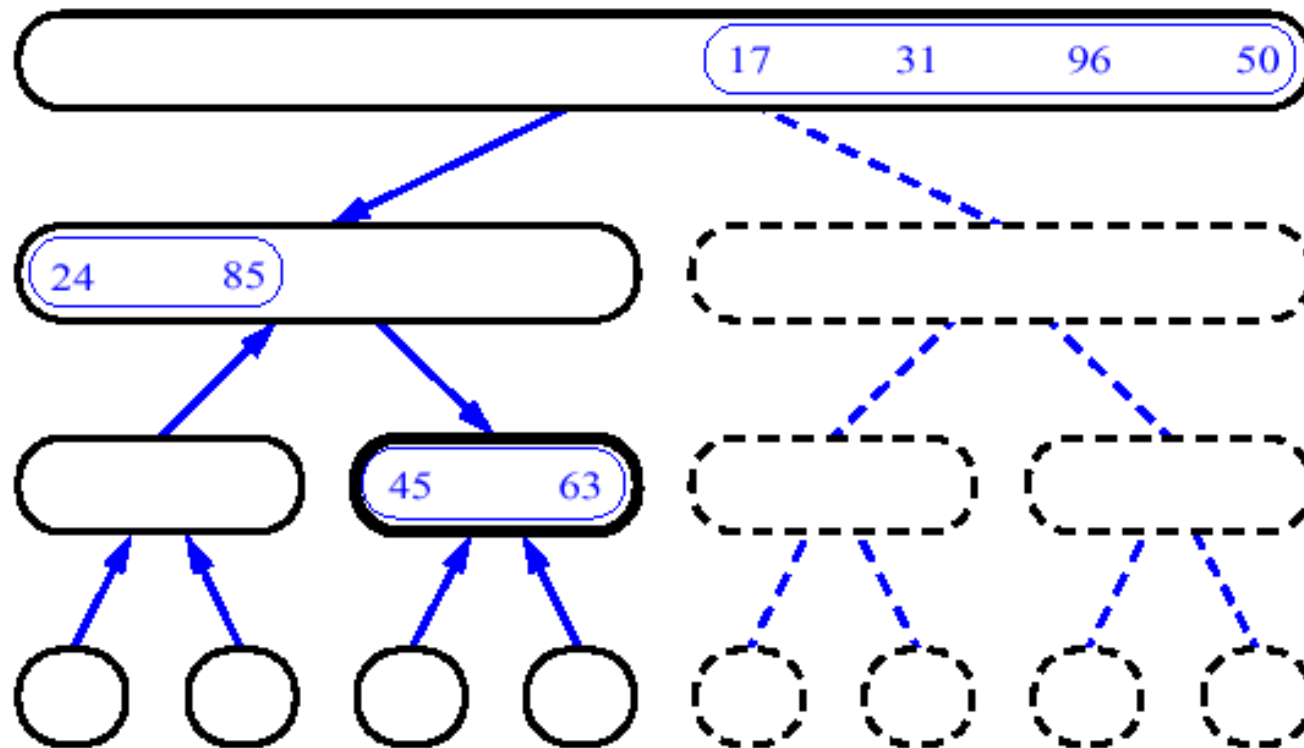
MergeSort (Example) - 13



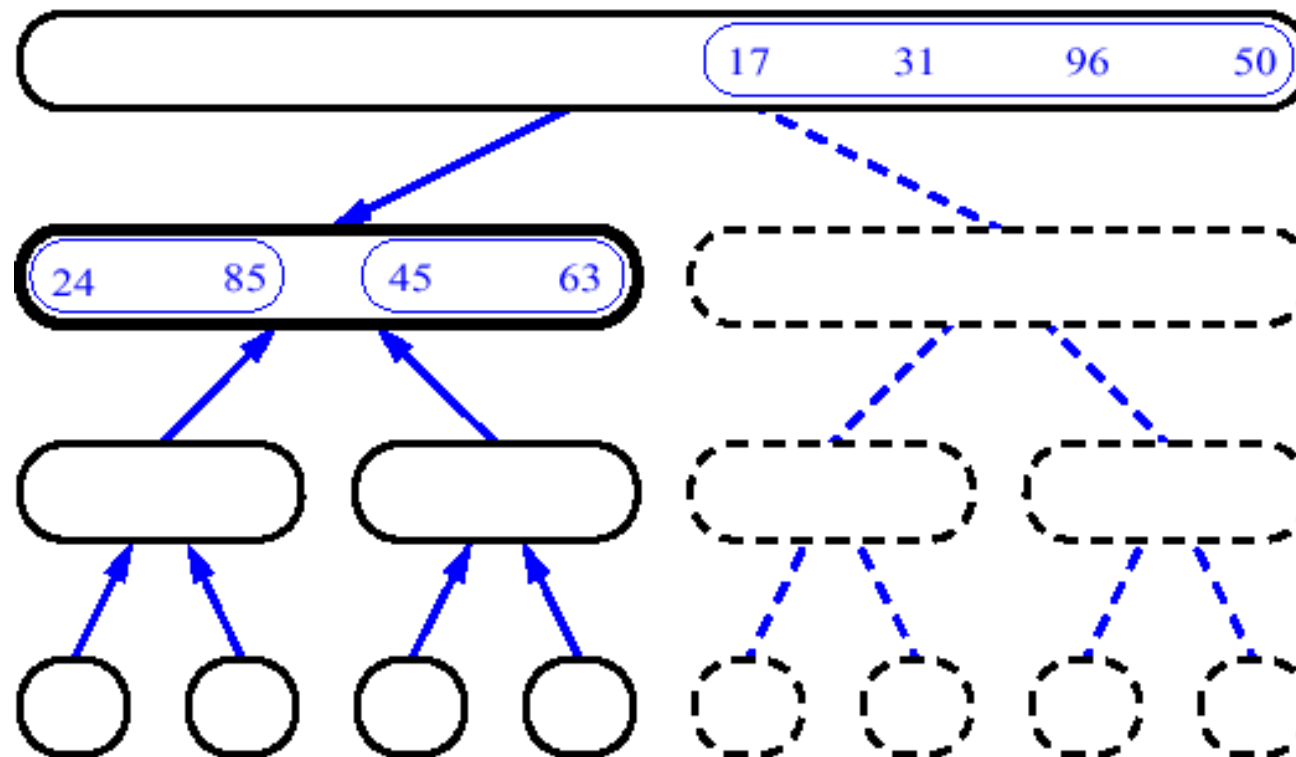
MergeSort (Example) - 14



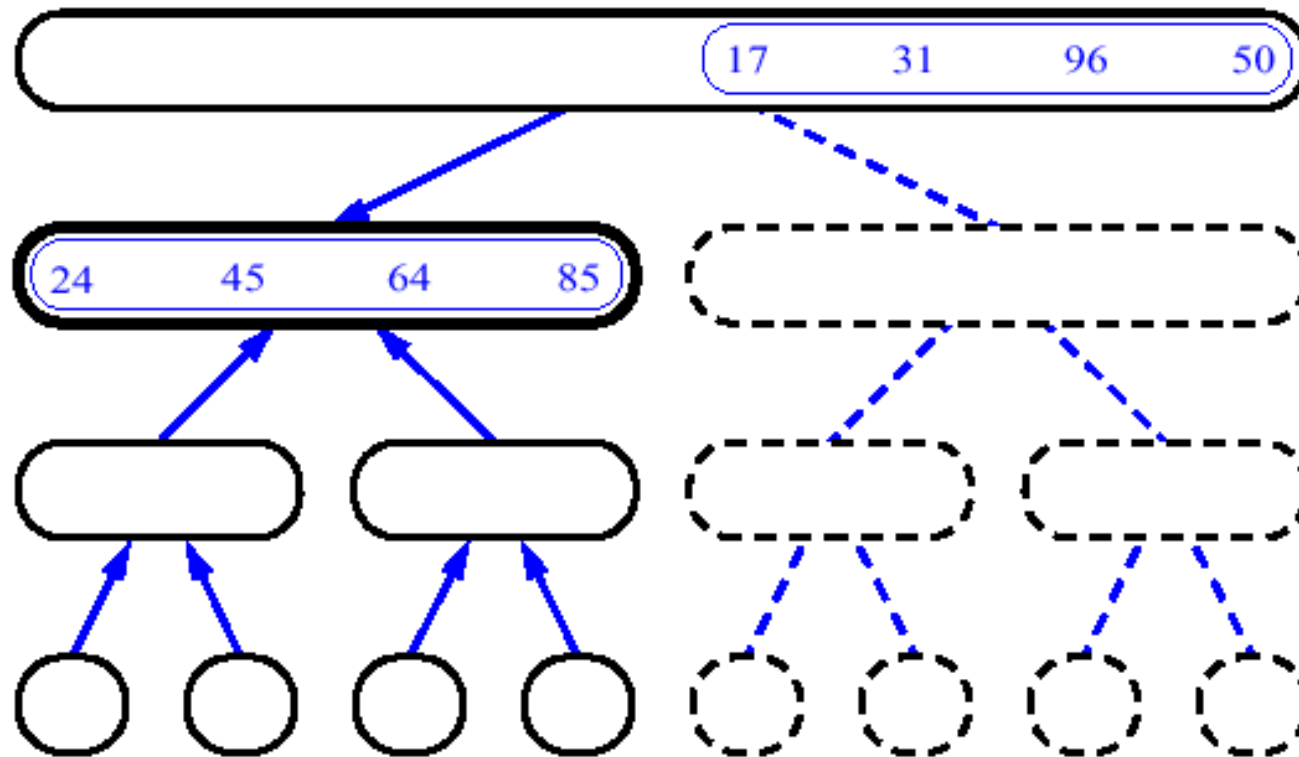
MergeSort (Example) - 15



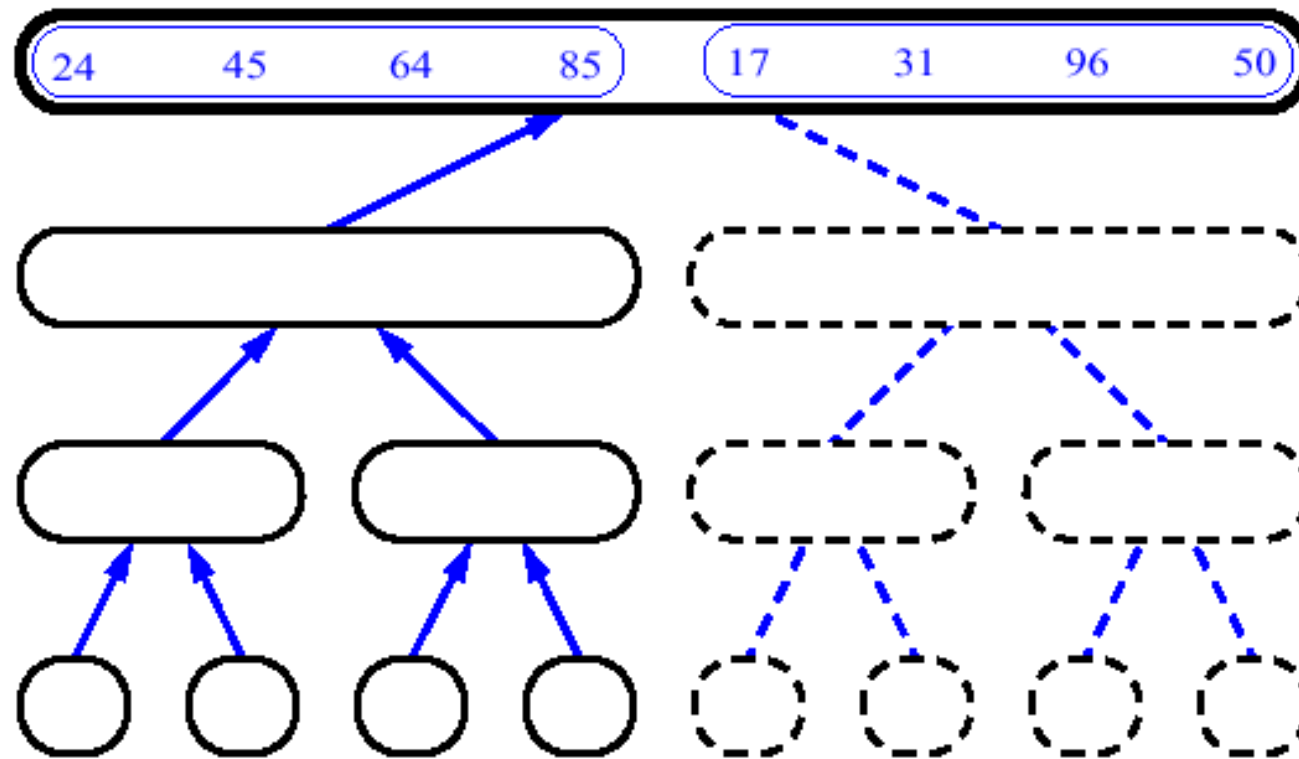
MergeSort (Example) - 16



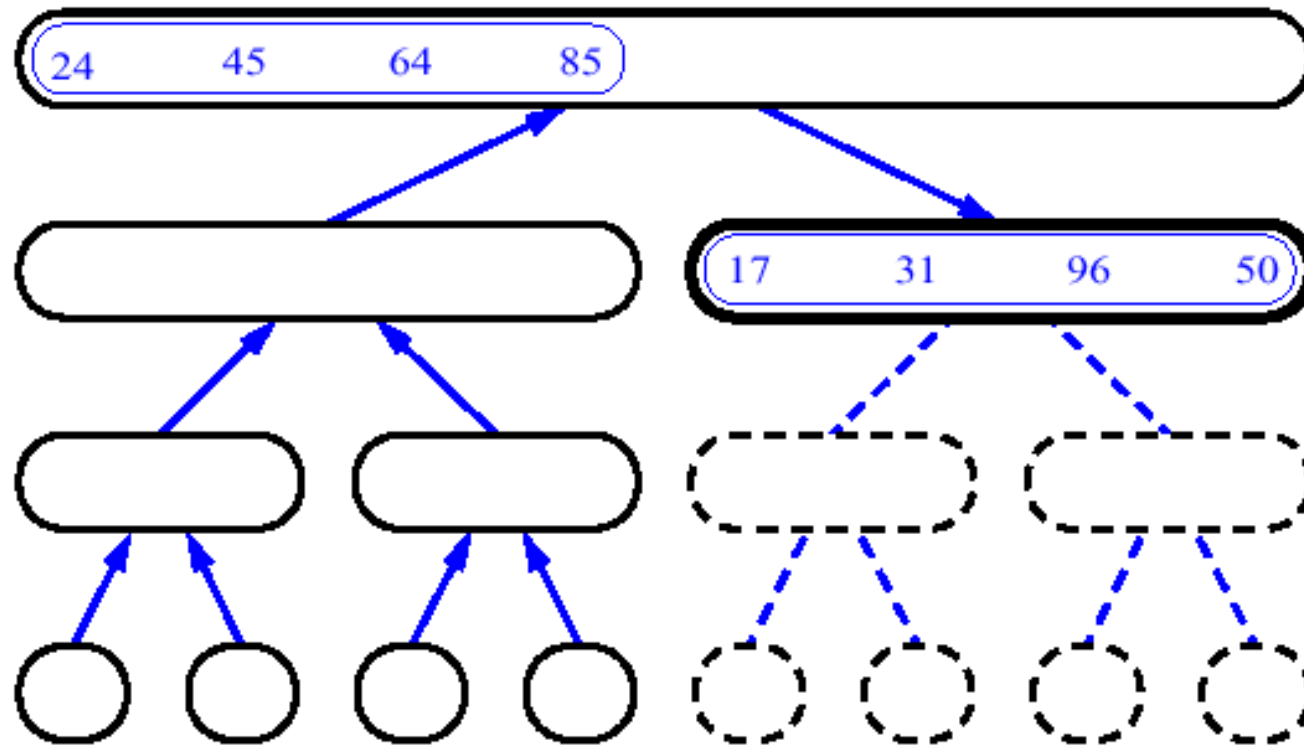
MergeSort (Example) - 17



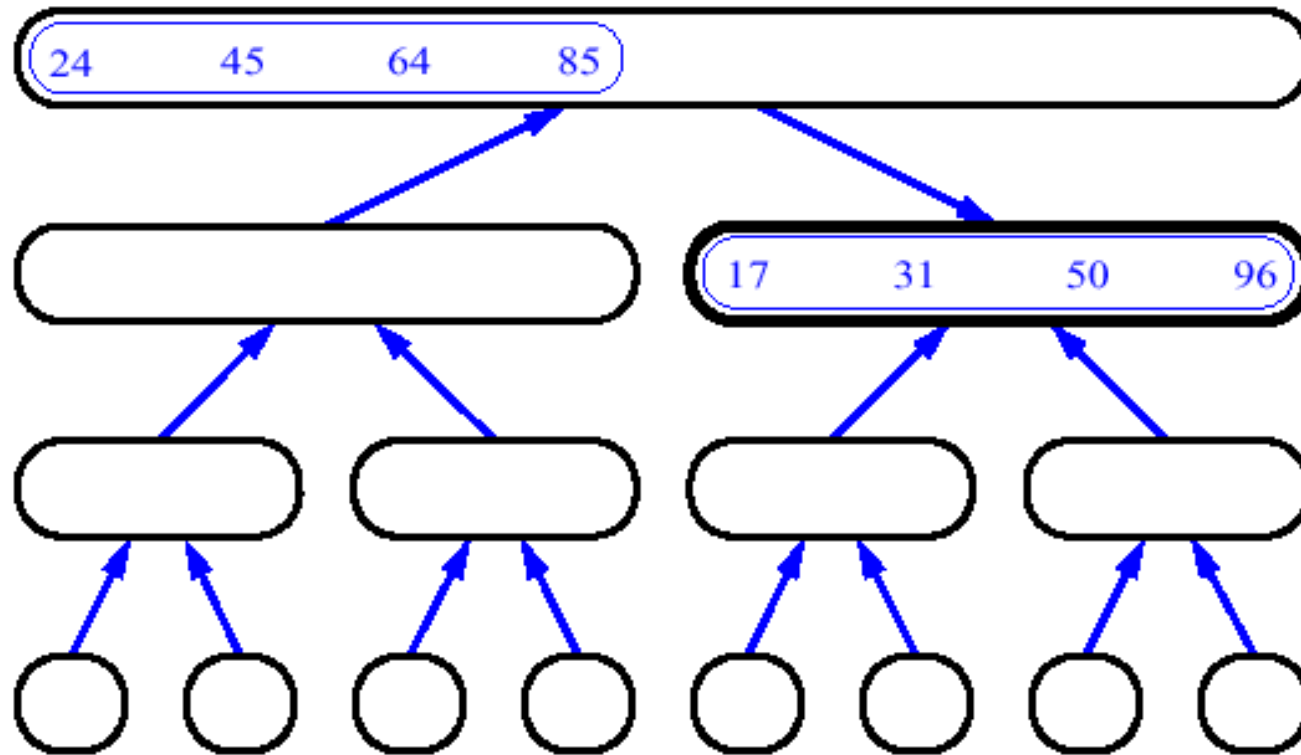
MergeSort (Example) - 18



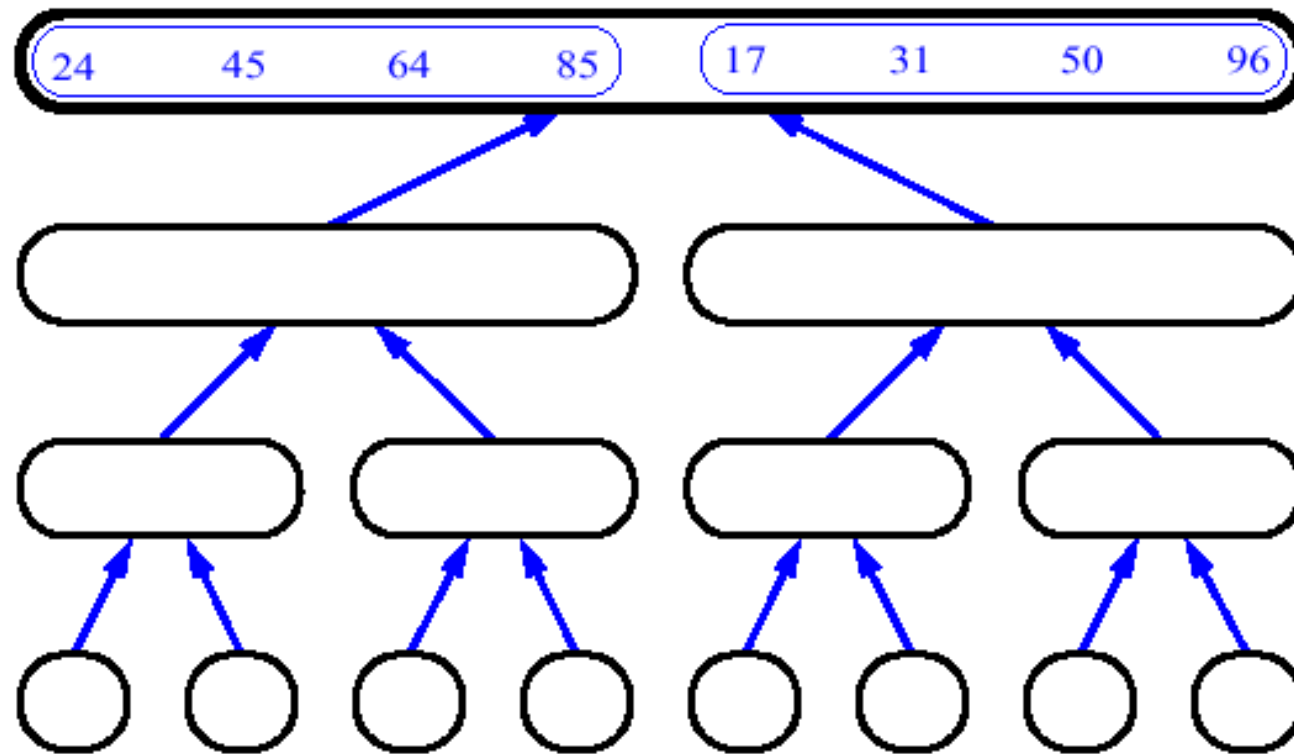
MergeSort (Example) - 19



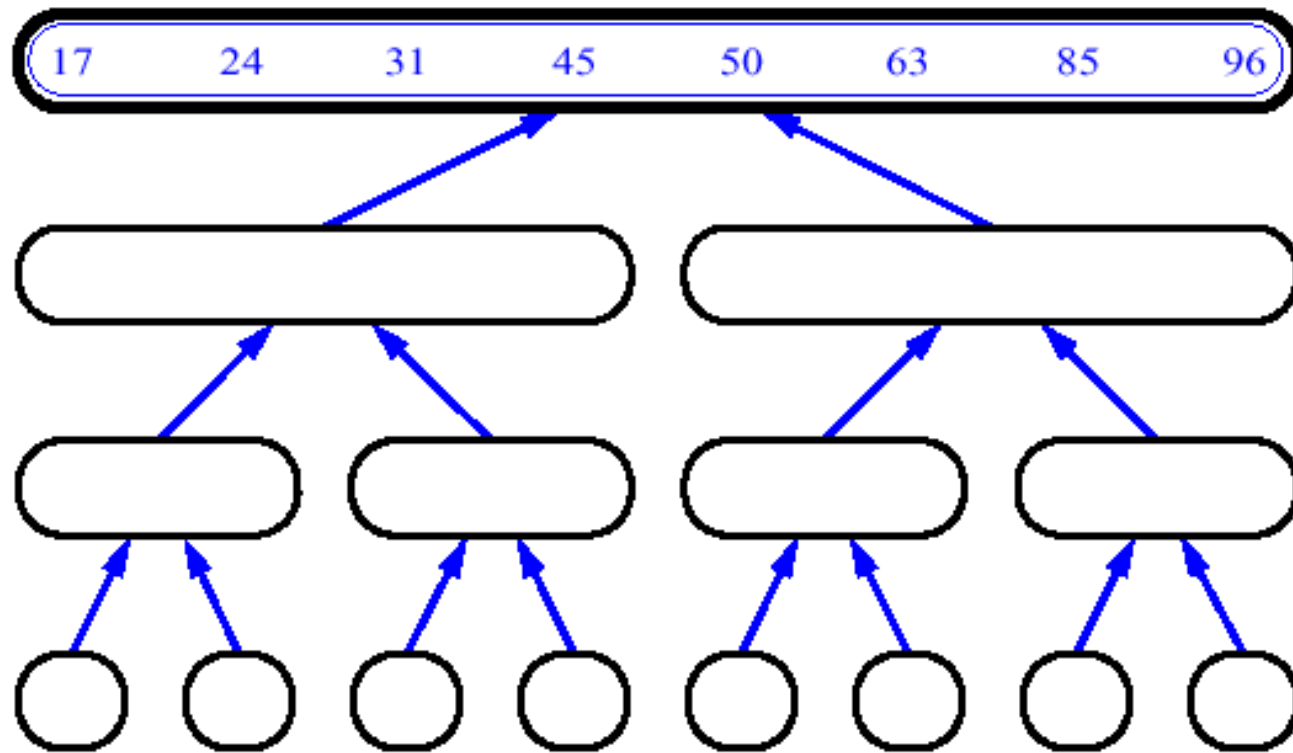
MergeSort (Example) - 20



MergeSort (Example) - 21



MergeSort (Example) - 22



14	23	45	98
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6	33	42	67
---	----	----	----

14	23	45	98
----	----	----	----

6	33	42	67
---	----	----	----

Merge

14	23	45	98
----	----	----	----

6	33	42	67
---	----	----	----

6

Merge

14	23	45	98
----	----	----	----

6	33	42	67
---	----	----	----

6	14
---	----

Merge

14	23	45	98
----	----	----	----

6	33	42	67
---	----	----	----

6	14	23
---	----	----

Merge

14	23	45	98
----	----	----	----

6	33	42	67
---	----	----	----

6	14	23	33
---	----	----	----

Merge

14	23	45	98
----	----	----	----

6	33	42	67
---	----	----	----

6	14	23	33	42
---	----	----	----	----

Merge

14	23	45	98
----	----	----	----

6	33	42	67
---	----	----	----

6	14	23	33	42	45
---	----	----	----	----	----

Merge

14	23	45	98
----	----	----	----

6	33	42	67
---	----	----	----

6	14	23	33	42	45	67
---	----	----	----	----	----	----

Merge

14	23	45	98
----	----	----	----

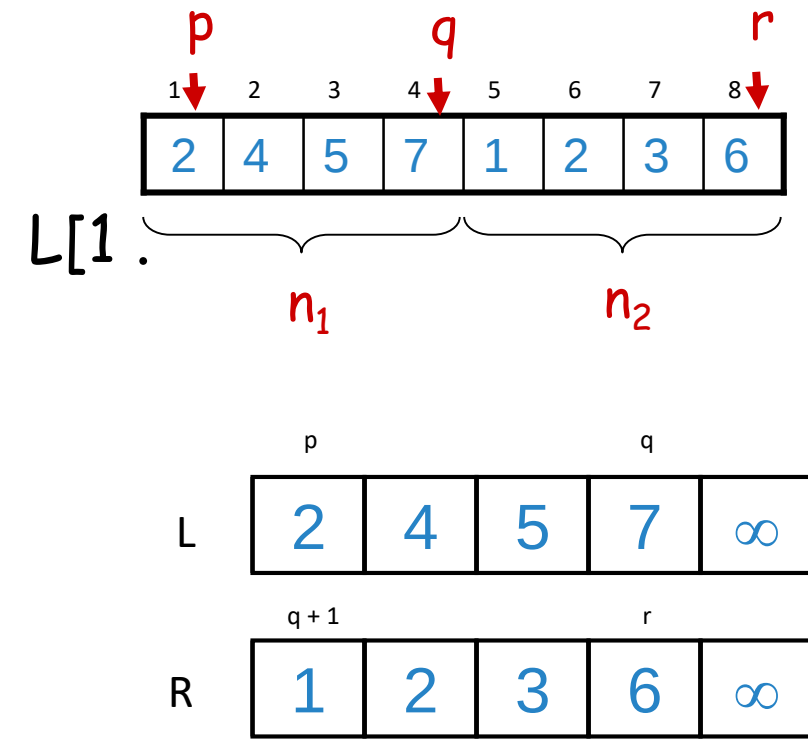
6	33	42	67
---	----	----	----

6	14	23	33	42	45	67	98
---	----	----	----	----	----	----	----

Merge

Alg.: MERGE(A, p, q, r)

1. Compute n_1 and n_2
2. Copy the first n_1 elements into $L[1 \dots n_1 + 1]$ and the next n_2 elements into $R[1 \dots n_2 + 1]$
3. $L[n_1 + 1] \leftarrow \infty$; $R[n_2 + 1] \leftarrow \infty$
4. $i \leftarrow 1$; $j \leftarrow 1$
5. **for** $k \leftarrow p$ **to** r
6. **do if** $L[i] \leq R[j]$
7. **then** $A[k] \leftarrow L[i]$
8. $i \leftarrow i + 1$
9. **else** $A[k] \leftarrow R[j]$
10. $j \leftarrow j + 1$



PSEUDOCODE

QUICK SORT

SORTING ALGORITHM

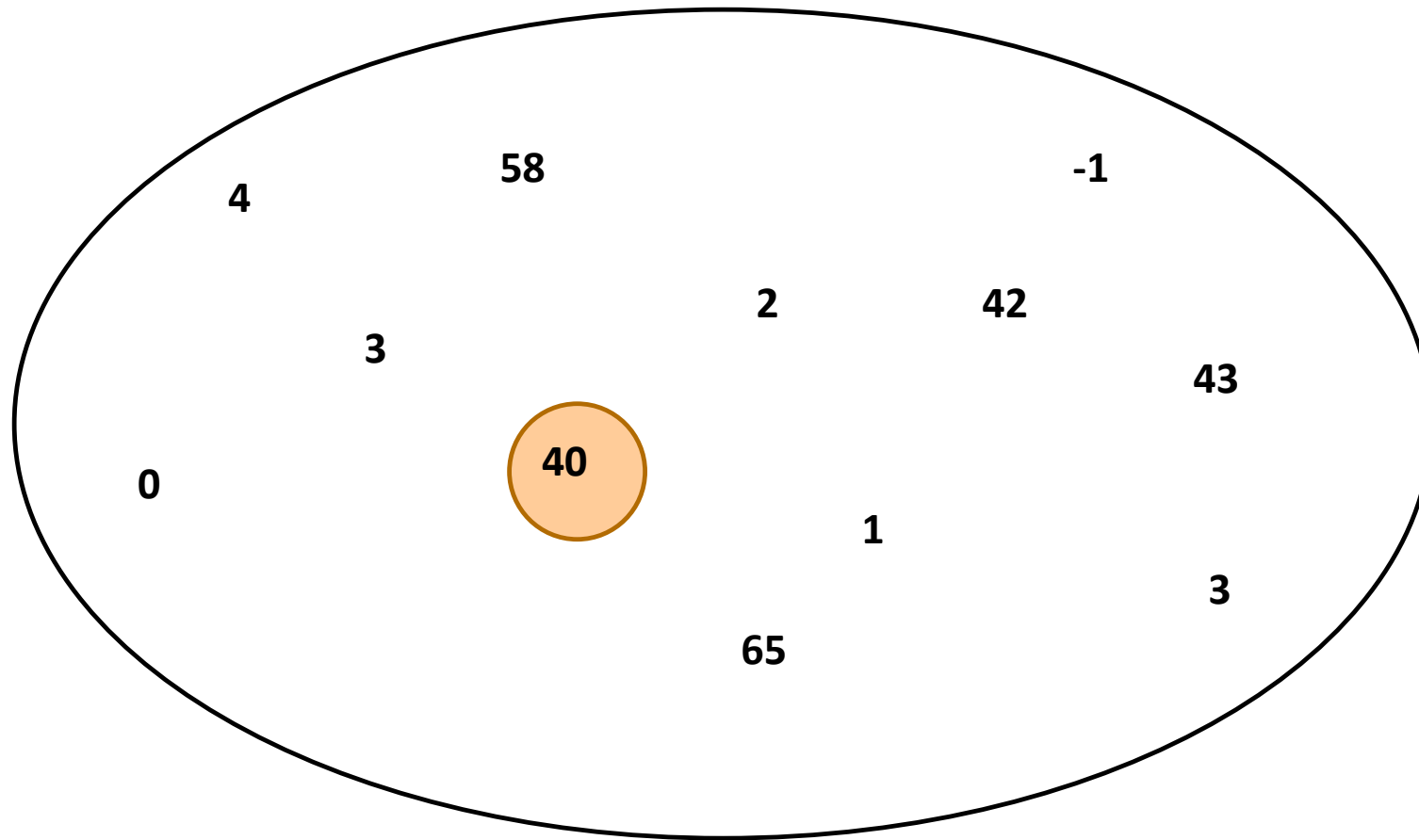
Quick sort: Ide dasar

Divide and conquer approach

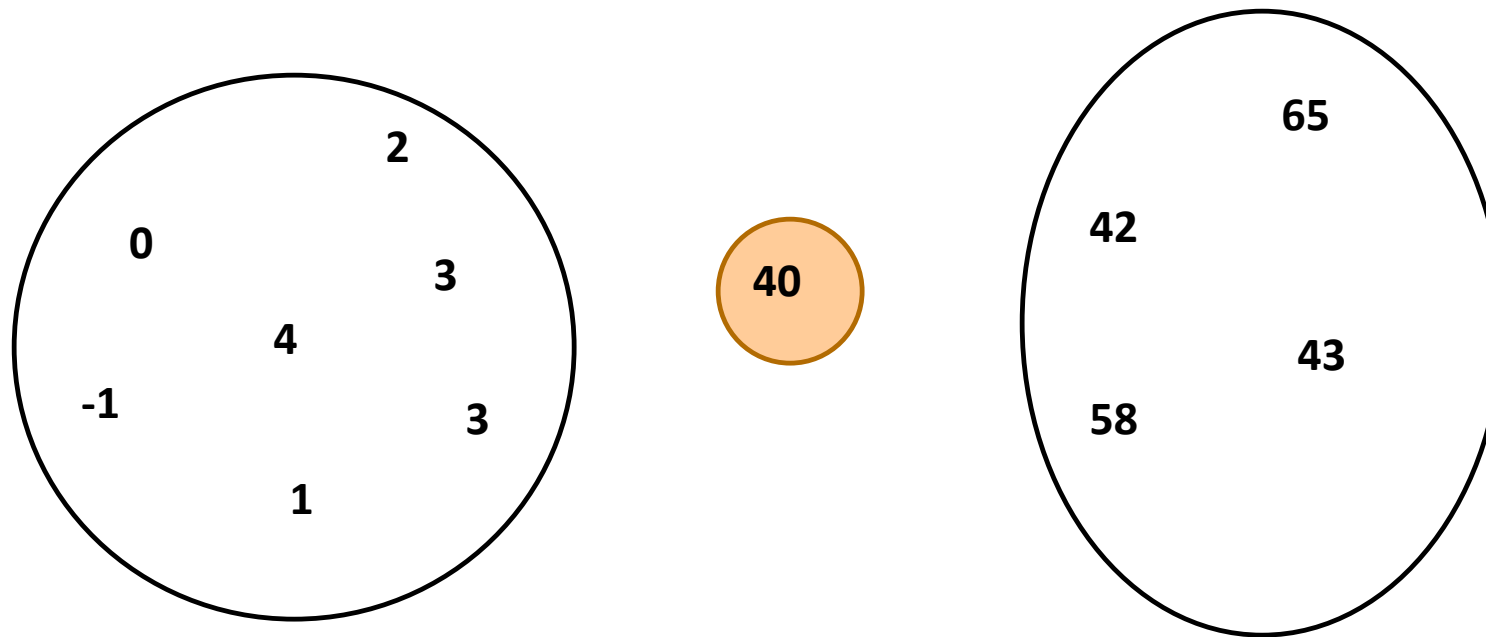
Algoritma *quickSort(S)*:

- Jika jumlah elemen dalam $S = 0$ atau 1 , return.
- Pilih sembarang elemen $v \in S$ – sebutlah **pivot**.
- Partisi $S - \{v\}$ ke dalam 2 bagian:
 - $L = \{x \in S - \{v\} \mid x \leq v\}$
 - $R = \{x \in S - \{v\} \mid x \geq v\}$
- Kembalikan nilai *quickSort(S)*, diikuti v , diikuti *quickSort(S)*.

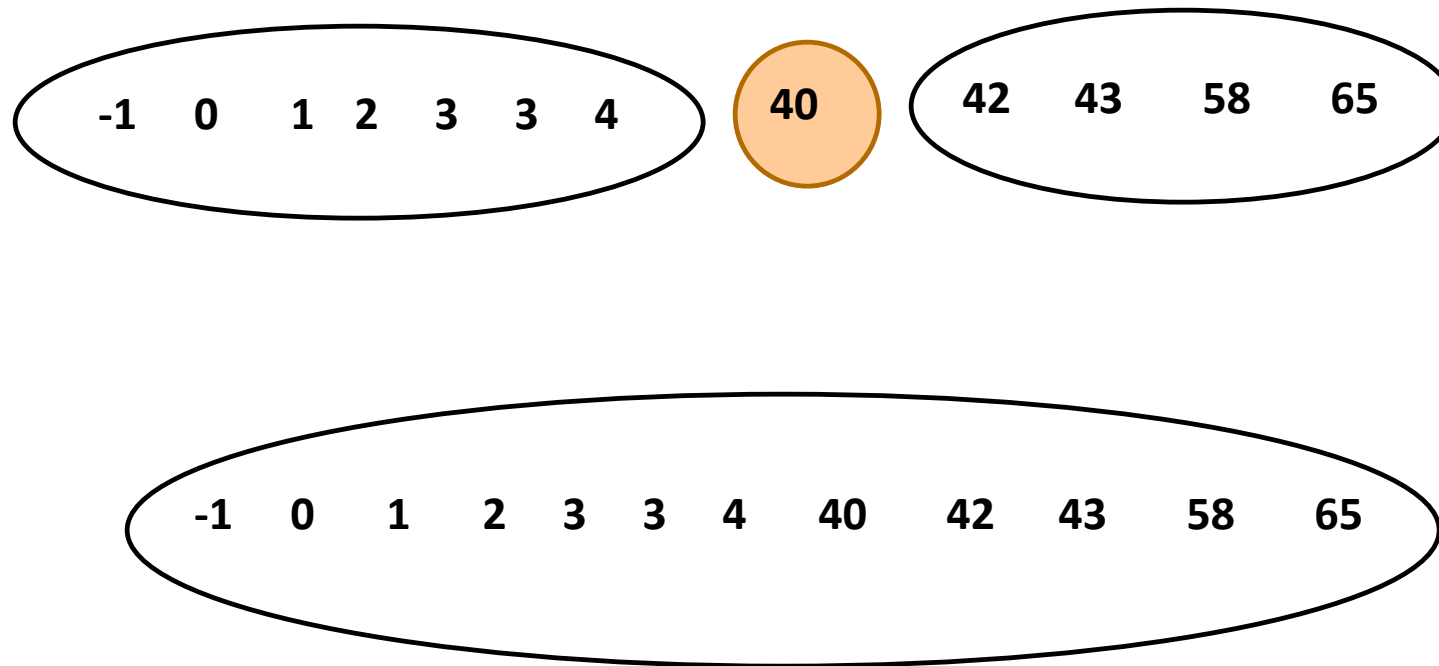
Quick sort: Pilih elemen *pivot*



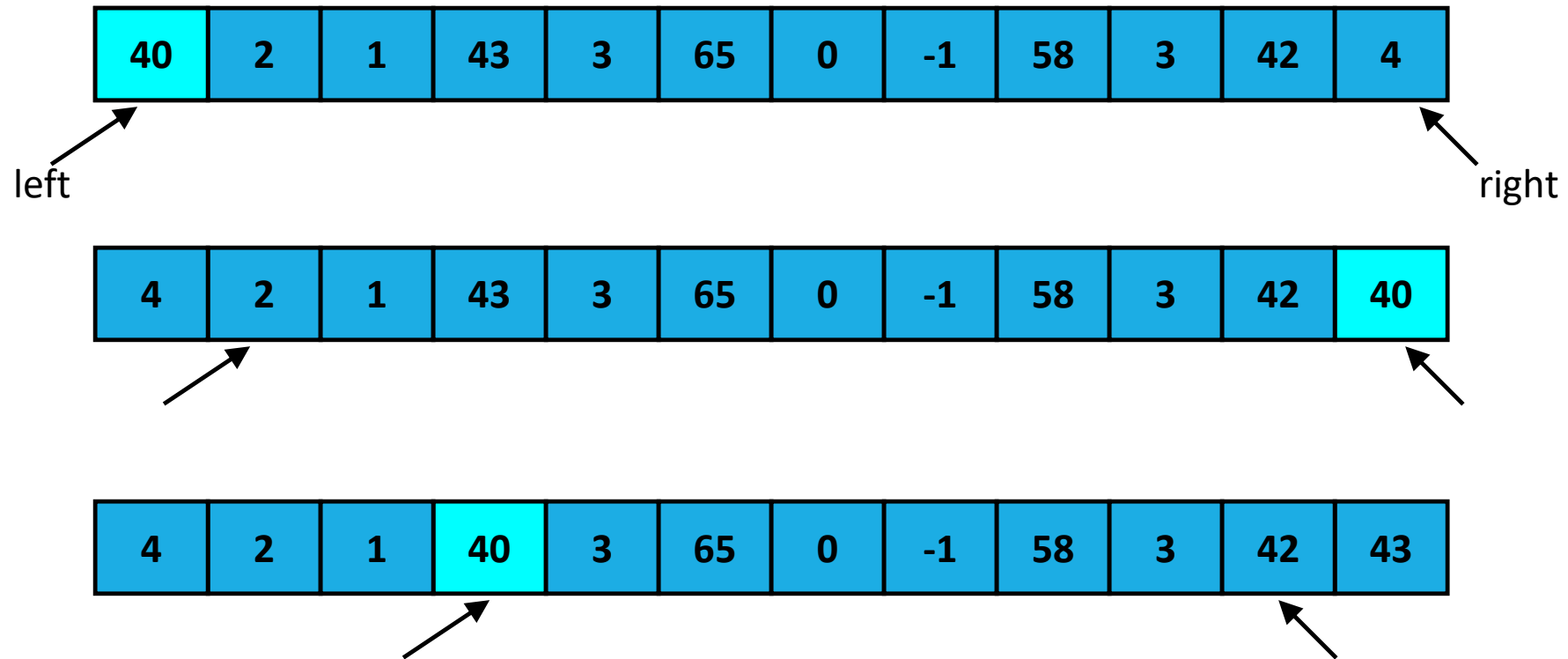
Quick sort: Partition



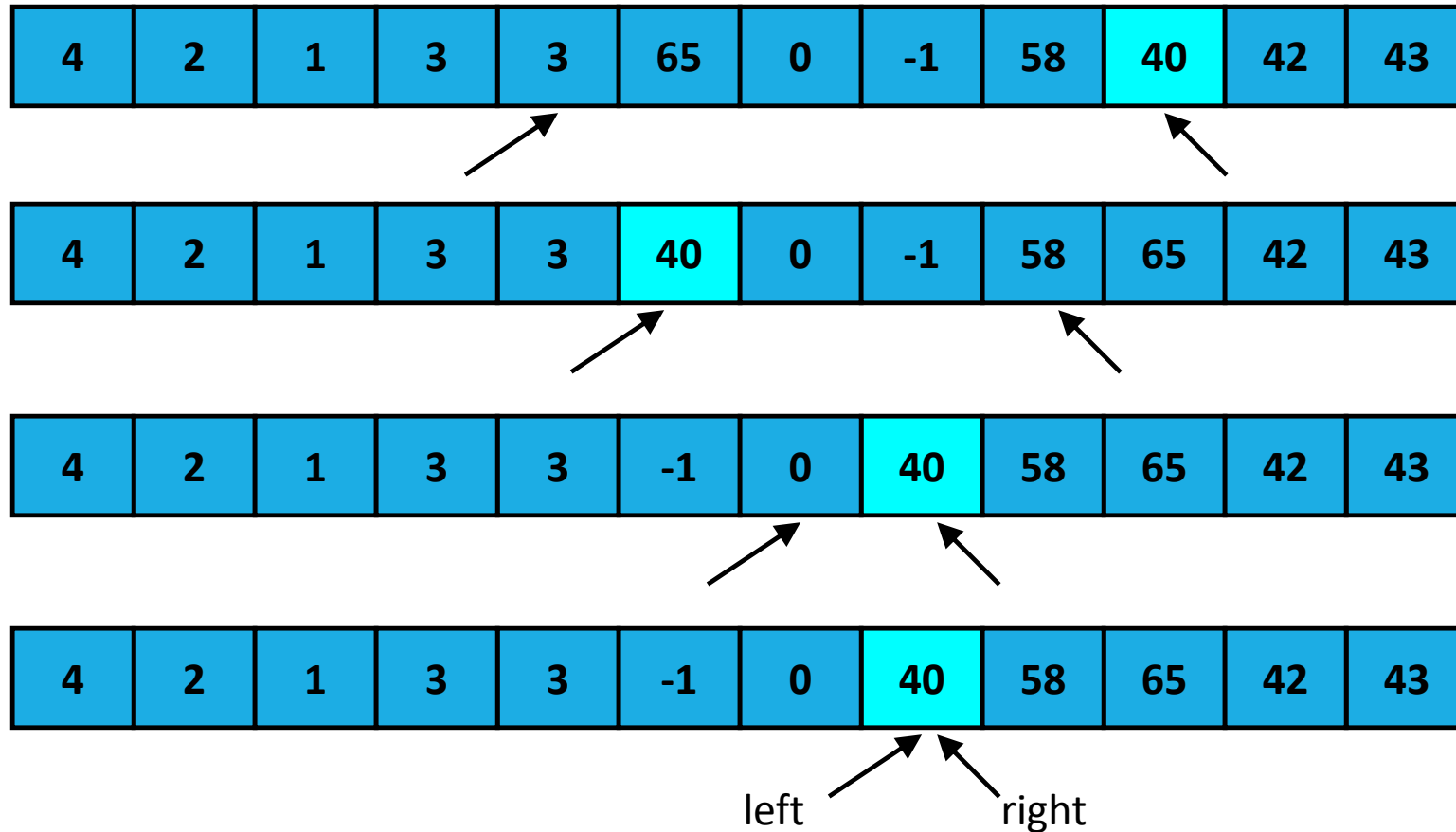
Quick sort: Sort scr. rekursif, gabungkan



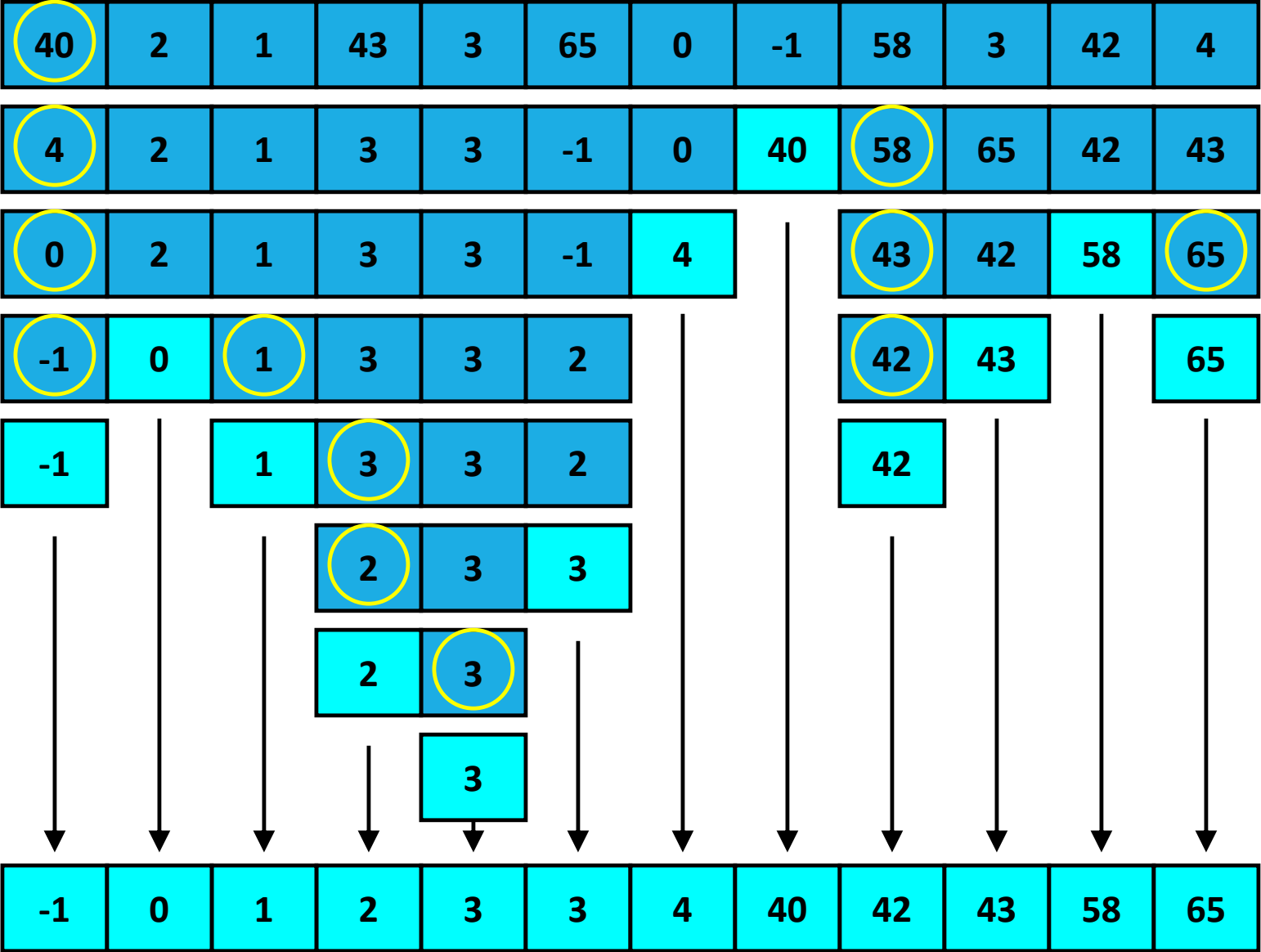
Quick sort: Partition algorithm 1



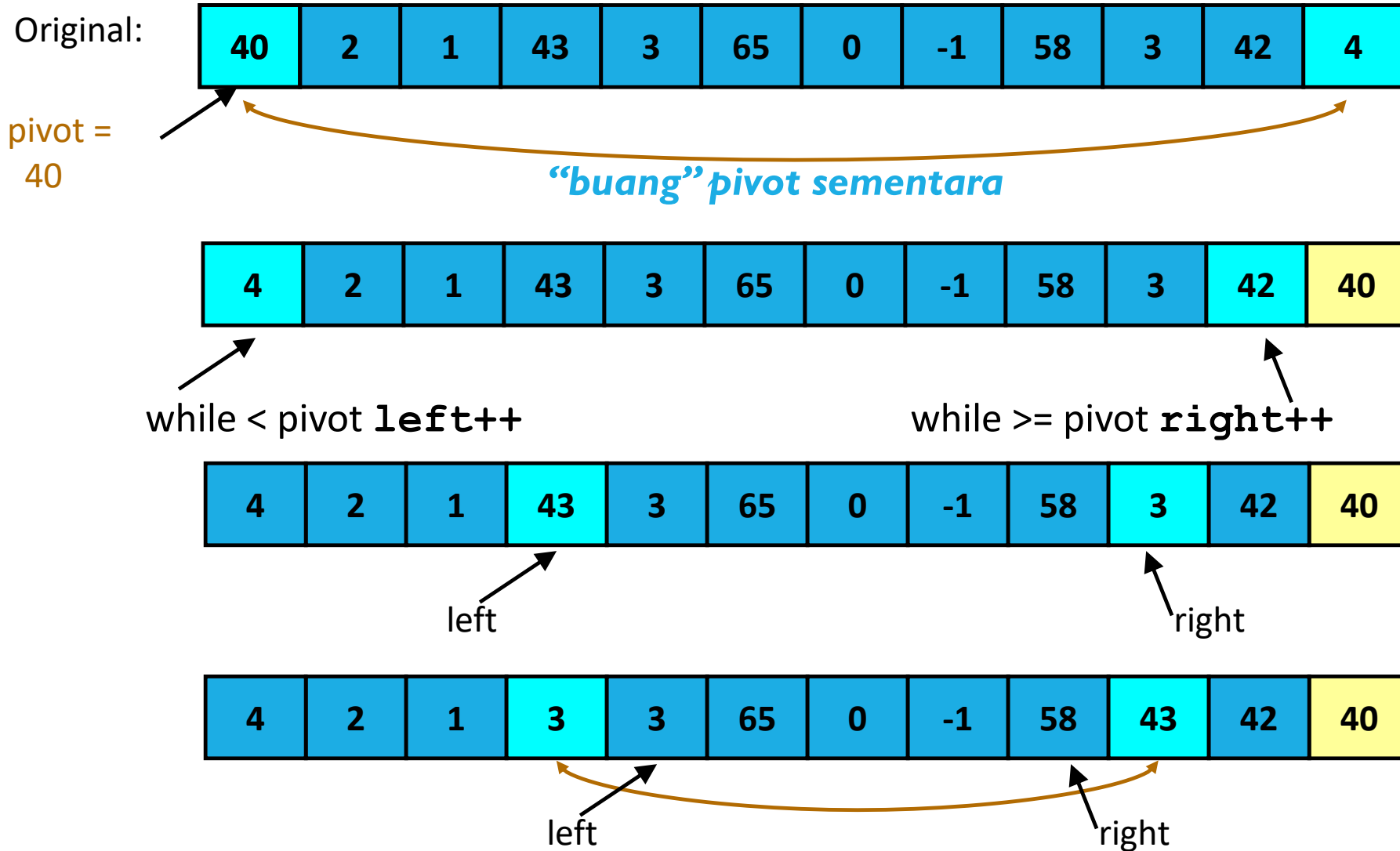
Quick sort: Partition algorithm 1



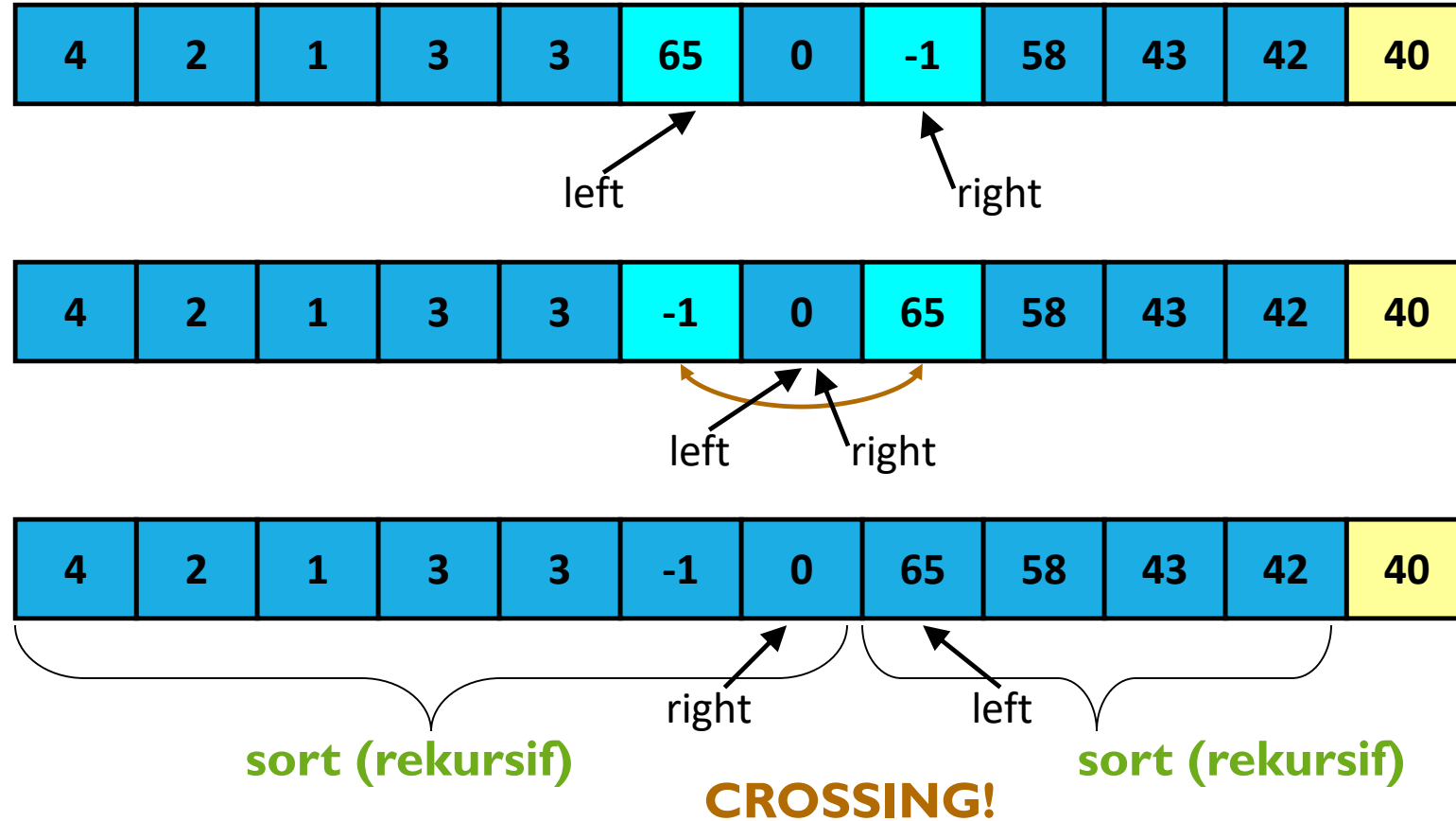
QUICK SORT : PARTITION ALGORITHM (1)



Quick sort: Partition algorithm 2



Quick sort: Partition algorithm 2



Quick sort: Implementasi

```
static void quickSort(int a[], int low, int high)
{
    if(high <= low) return; // base case
    pivot = choosePivot(a); // select "best" pivot

    int i=low, j=high-1;
    swap(a,pivot,a[j]); // move pivot out of the way
    while(i <= j)
    {
        // find large element starting from left
        while(i<high && a[i]<pivot) i++;

        // find small element starting from right
        while(j>low && a[j]>=pivot) j--;

        // if the indexes have not crossed, swap
        if(i>j) swap(a, i, j);
    }
    swap(a,i,high-1); // restore pivot
    quickSort(a,low,i-1); // sort small elements
    quickSort(a,i+1,high); // sort large elements
}
```

Quick sort: Memilih pivot

Pivot ideal:

- Elemen media

Yang biasa dijadikan calon pivot:

- Elemen pertama
- Elemen terakhir
- Elemen di tengah-tengah
- Median dari ketiga elemen tsb.

Source

<http://www.cs.sfu.ca/CourseCentral/307/jmanuch/lec/MergeSort.ppt>

<http://www.cse.unr.edu/~bebis/CS477/Lect/MergesortQuickSort.ppt>

Slide Kuliah Fasilkom UI

Next....

- Bucket Sort
- Shell Sort
- Radix Sort
- External Sort